

## Conformational Transitions and Charge Translocation by the Na,K Pump: Comparison of Optical and Electrical Transients Elicited by ATP-Concentration Jumps

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**Summary.** The electrogenic properties of the Na,K-ATPase were studied by correlating transient electrical events in the pump molecule with conformational transitions elicited by an ATP-concentration jump. Flat membrane fragments containing a high density ( $\sim 8000 \mu\text{m}^{-2}$ ) of oriented Na,K-ATPase molecules were bound to a planar lipid bilayer acting as a capacitive electrode. ATP was released in the medium from a photolabile inactive ATP derivative ("caged" ATP) by a 40- $\mu\text{sec}$  light flash. Electrical signals resulting from transient charge movements in the protein under single-turnover conditions were recorded in the external measuring circuit. In parallel experiments carried out under virtually identical conditions, the fluorescence of membrane fragments containing Na,K-ATPase with covalently-bound 5-iodoacetamido-fluorescein (5-IAF) was monitored after the ATP-concentration jump. When the medium contained  $\text{Na}^+$ , but no  $\text{K}^+$ , the fluorescence of the 5-IAF-labeled protein decreases monotonously after release of ATP. In the experiments with membrane fragments bound to a planar bilayer, a transient pump current was observed which exhibited virtually the same time behavior as the fluorescence decay. This indicates that optical and electrical transients are governed by the same rate-limiting reaction step. Experiments with chymotrypsin-modified Na,K-ATPase suggest that both the fluorescence change as well as the charge movement are associated with the deocclusion of  $\text{Na}^+$  and release to the extracellular side. In experiments with  $\text{Na}^+$ -free  $\text{K}^+$  media, a large inverse fluorescence change is observed after the ATP-concentration jump, but no charge translocation can be detected. This indicates that deocclusion of  $\text{K}^+$  is an electrically silent process.

**Key Words** Na,K-ATPase · active transport · electrogenic pumps · fluorescence probes · conformational transitions · caged ATP

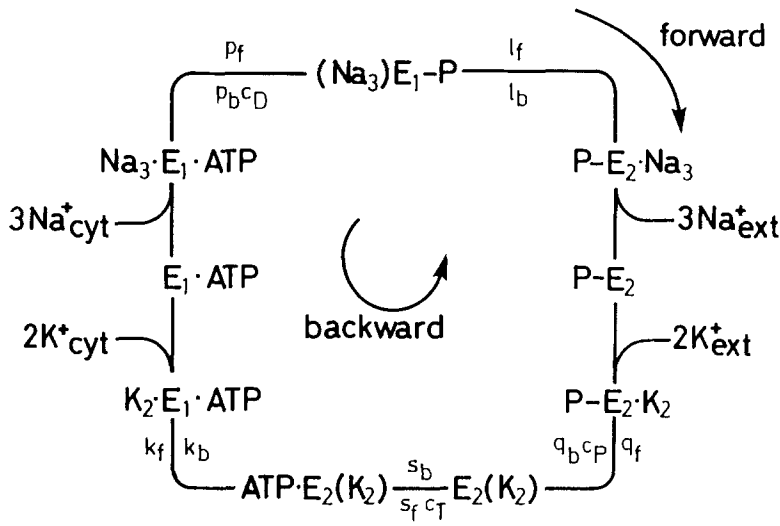
### Introduction

The Na,K pump of the plasma membrane of animal cell utilizes free energy of ATP hydrolysis for uphill transport of  $\text{Na}^+$  and  $\text{K}^+$  (Skou, 1975; Robinson & Flashner, 1979; Cantley, 1981; Schuurmans-Stekhoven & Bonting, 1981; Jørgensen, 1982; Glynn, 1985; Kaplan, 1985; Jørgensen & Andersen, 1988). In its normal mode of operation, the pump

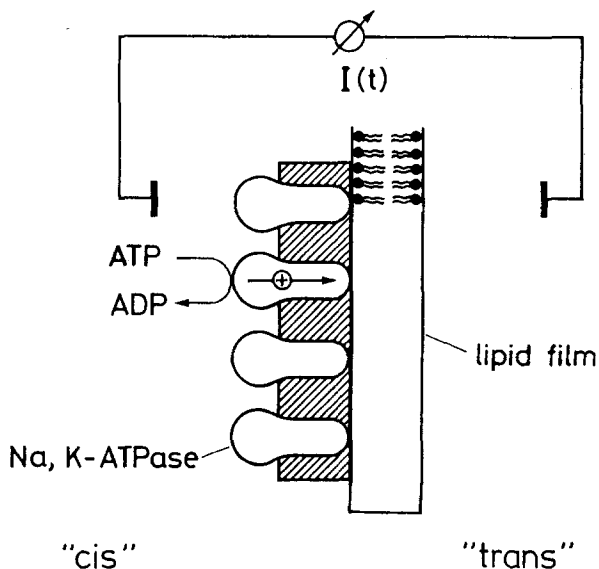
performs a cycle of conformational transitions and ion-binding and -release steps. Spectroscopic studies as well as proteolysis experiments indicate that the enzyme can assume two principal conformations designated  $E_1$  and  $E_2$ . Form  $E_1$  has the ion-binding sites facing the cytoplasm and is stabilized by  $\text{Na}^+$ ; form  $E_2$  has the ion-binding sites facing the extracellular medium and is stabilized by  $\text{K}^+$ . From enzymatic and transport studies the reaction cycle represented in Fig. 1 has been proposed (Albers, 1967; Post, Hegyvary & Kume, 1972; Cantley et al., 1984). When the protein is phosphorylated in state  $E_1$  by ATP,  $\text{Na}^+$  becomes "occluded," i.e., trapped inside the protein ( $\text{Na}_3 \cdot E_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)E_1-P$ ). After transition to conformation  $E_2$ ,  $\text{Na}^+$  is released and  $\text{K}^+$  is bound. This leads to dephosphorylation of the protein and occlusion of  $\text{K}^+$ . The original state is restored by transition to conformation  $E_1$  and release of  $\text{K}^+$  to the cytoplasmic side.

The kinetics of transitions between conformations  $E_1$  and  $E_2$  may be investigated by time-resolved fluorescence measurements, using intrinsic or extrinsic fluorescent probes (Karlsh & Yates, 1978; Karlsh, Yates & Glynn, 1978a,b; Karlsh, 1980; Hegyvary & Jørgensen, 1981; Skou & Es-mann, 1981, 1983; Skou, 1982; Taniguchi, Suzuki & Iida, 1983; Rephaeli, Richards & Karlsh, 1986a,b; Glynn et al., 1987; Suzuki, Taniguchi & Iida, 1987). These studies have shown that transitions from  $E_1$  to  $E_2$  may be induced by changing the medium from a sodium-rich to a potassium-rich solution (and vice versa), or by phosphorylation. From the time course of fluorescence changes, estimates for the rate constants of the reaction cycle may be obtained.

An entirely different possibility for studying the kinetics of the pumping process consists in analyzing electrical signals resulting from charge translocations in the pump molecule. Flat membrane fragments containing a high density (several thousand



**Fig. 1.** Post-Albers scheme for the pumping cycle of Na,K-ATPase (adapted from Cantley et al., 1984).  $E_1$  and  $E_2$  are conformations of the enzyme with ion binding sites exposed to the cytoplasm and the extracellular medium, respectively. In the "occluded" states  $(Na_3)E_1-P$  and  $E_2(K_2)$  the bound ions are unable to exchange with the aqueous phase. Dashes indicate covalent bonds and dots indicate noncovalent bonds.  $p_f$ ,  $l_f$ ,  $q_f$ ,  $s_f c_T$ ,  $k_f$  and  $p_b c_D$ ,  $k_b$ ,  $s_b$ ,  $q_b c_P$ ,  $l_b$  are rate constants for transitions in forward and backward direction, respectively.  $c_T$ ,  $c_D$  and  $c_P$  are cytoplasmic concentrations of ATP, ADP and  $P_i$  (inorganic phosphate)



**Fig. 2.** Planar lipid bilayer with adsorbed Na,K-ATPase membrane fragments. When a suspension of flat membrane fragments 0.1–1  $\mu\text{m}$  in diameter containing a high density ( $10^3$ – $10^4 \mu\text{m}^{-2}$ ) of oriented Na,K-ATPase molecules is added to the aqueous medium, membrane fragments become bound to the lipid bilayer, some with the cytoplasmic side facing the solution. Flash-induced release of ATP from a photolabile ATP derivative ("caged" ATP) elicits a transient current  $I(t)$  in the external measuring circuit

per  $\mu\text{m}^2$ ) of oriented Na,K-ATPase molecules may be bound to a planar lipid bilayer acting as a capacitive electrode (Fig. 2). When ATP is released within a few msec to the medium by flash excitation of a photolabile inactive ATP-derivative ("caged" ATP) current signals can be recorded in the external measuring circuit in the time range of 10–100 msec (Fendler et al., 1985; Apell, Borlinghaus & Lauger,

1987; Borlinghaus, Apell & Lauger, 1987; Fendler, Grell & Bamberg, 1987; Nagel et al., 1987; Borlinghaus & Apell, 1988). These transient currents reflect charge movements in the protein induced by phosphorylation. Blocking the deocclusion step  $(Na_3)E_1-P \rightarrow P-E_2 \cdot Na_3$  by chymotrypsin modification of the protein has given evidence that the main electrogenic step in the sodium limb of the cycle is deocclusion of  $Na^+$  to the extracellular side (Borlinghaus et al., 1987).

An important problem in the understanding of the kinetic behavior of the Na,K-pump is the question, how the charge movements which give rise to the transient currents are correlated with the spectroscopically-detected conformational changes. In the following, we describe experiments in which transient fluorescence changes of 5-iodoacetamido-fluorescein-labeled Na,K-ATPase (Kapakos & Steinberg, 1982, 1986a,b; Glynn et al., 1987; Fortes & Aguilar, 1988; Steinberg & Karlsh, 1989; Tyson et al., 1989) have been recorded after an ATP-concentration jump. In parallel experiments with the same ATPase preparation, electrical signals have been measured in the lipid bilayer system after flash release of ATP from "caged" ATP. It will be shown that valuable kinetic information can be obtained by comparison of the optical and the electrical signals.

## Materials and Methods

### MATERIALS

L-1,2-diphytanoyl-3-phosphatidylcholine was obtained from Avanti Polar Lipids, Birmingham, AL; sodium dodecylsulfate (SDS) from Pierce Chemical (Rockford, IL) and sodium cholate from Merck (Darmstadt). Phosphoenolpyruvate, pyruvate ki-

nase, lactate dehydrogenase, luciferin, luciferase, NADH and ATP (disodium salt, Sonderqualität) were from Boehringer (Mannheim).  $\alpha$ -chymotrypsin (type II), apyrase VI and ouabain were purchased from Sigma and 5-iodoacetamidofluorescein (5-IAF) from Molecular Probes (Eugene, OR). In the experiments in nominal absence of  $K^+$ , NaCl was used in Suprapur quality (Merck). All other reagents were analytical grade. Sephadex G25 and G100 were obtained from Serva (Heidelberg).

$P^3$ -1-(2-nitro)phenylethyladenosine-5'-triphosphate ("caged" ATP) was synthesized by K. Janko using a modified version of the method of Kaplan, Forbush and Hoffman (1978). The purity of the product was checked by HPLC. The compound was stored as tetramethylammonium salt in the dark at  $-40^\circ\text{C}$ .

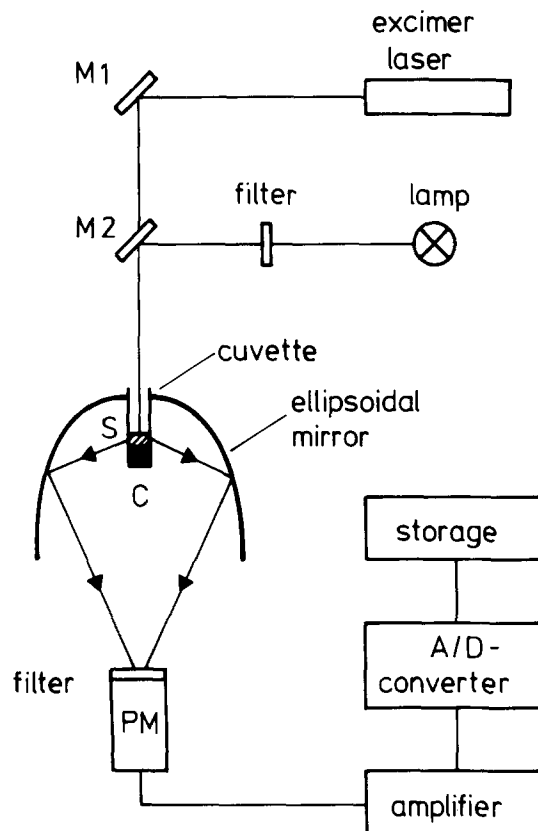
### ENZYME PREPARATION AND FLUORESCENCE LABELING

Na,K-ATPase was prepared from the outer medulla of rabbit kidneys using procedure C of Jørgensen (1974). This method yields purified enzyme in the form of membrane fragments containing about 0.6 mg phospholipid and 0.2 mg cholesterol per mg protein (Jørgensen, 1974, 1982). The specific ATPase activity was determined by the pyruvate kinase/lactate dehydrogenase assay (Schwartz et al., 1971) and the protein concentration by the Lowry method (Lowry et al., 1951), using bovine serum albumin as a standard. For most preparations the specific activity was in the range between 1500 and 2200  $\mu\text{mol P}$ , per hr and mg protein at  $37^\circ\text{C}$ , corresponding to a turnover rate of 120–170  $\text{sec}^{-1}$  (based on a molar mass of 280,000 g/mol). The suspension of Na,K-ATPase-rich membrane fragments (about 3 mg protein per ml) in buffer (25 mM imidazole, pH 7.5, 1 mM EDTA, 10 mg/ml saccharose) was frozen in samples of 100  $\mu\text{l}$ ; in this form the preparation could be stored for several months at  $-70^\circ\text{C}$  without significant loss of activity.

Fluorescence labeling of the enzyme was performed by incubating 200–300  $\mu\text{g}$  of the enzyme for 48 hr at  $4^\circ\text{C}$  with a solution containing 100  $\mu\text{M}$  5-IAF, 10 mM  $K_2SO_4$  and 50 mM imidazole sulfate, pH 7.5 (Kapakos & Steinberg, 1982). The labeled enzyme was separated from unbound dye by passing the reaction mixture through a 3-cm long Sephadex G-25 column.

### FLUORESCENCE MEASUREMENTS

For high-resolution recording of time-dependent fluorescence signals the set-up represented in Fig. 3 was used. The fluorescence of membrane-bound 5-IAF was excited by light from a 250-W tungsten-halogen lamp. The light beam passed through a water-filled infrared-absorbing filter (not shown) and an interference filter (peak wavelength 481 nm, half-width 14 nm; Anders, Nabburg, FRG). The exciting light was focussed into the cylindrical quartz cuvette (internal diameter 7.8 mm). The solution layer in the cuvette had a height of 5–6 mm. The bottom plate of the cuvette was coated at the outer surface with a reflecting layer; it was in contact with a thermostated metal console of the same diameter as the cuvette. Fluorescence light emitted from the cuvette was collected by an ellipsoidal mirror (Melles Griot, Zevenaar, Netherlands) and focussed onto the cathode of a side-on photomultiplier (Hamamatsu, Mod. R928). Cuvette and photomultiplier were mounted in such a way that the light-emitting part of the cuvette was in one focal point of the mirror and the photocathode in the other. In this way efficient light collection from a large solid angle was achieved. A second interference



**Fig. 3.** Set-up for time-resolved fluorescence measurements. The cylindrical glass cuvette containing the sample (S) is mounted on a thermostated metal console (C). Fluorescence of the sample is excited by light from a tungsten-halogen lamp. The light emitted by the sample is collected by an ellipsoidal mirror and focussed onto the cathode of the photomultiplier (PM). The light-emitting part of the cuvette is located in one focal point of the mirror and the photocathode in the other. The photomultiplier signal is amplified, digitized in an analog-to-digital converter and stored in the memory of the Compaq-386 computer. ATP is released from "caged" ATP by a 10-nsec pulse from an excimer laser. The laser beam enters the cuvette through a hole in mirror M2

filter (peak wavelength 522.5 nm, half-width 12.6 nm) was mounted in front of the photomultiplier.

The voltage for the photomultiplier was delivered by a highly stabilized power supply (John Fluke, Seattle, Mod. 405B). The current signal of the photomultiplier was converted to voltage and amplified in three stages. The input stages of the amplifiers were protected by diodes against overload. This was necessary since the 308-nm flash excited strong fluorescence and phosphorescence in some of the optical elements (lenses and cuvette). The total recovery time of the recording system after the flash was given by the decay time constant of the phosphorescence ( $\sim 1$  msec). For the compensation of the stationary fluorescence signal prior to the flash a differential amplifier was used. The output signal of the differential amplifier was amplified ten times and passed through an active low-pass filter. In most experiments the bandwidth was 1 kHz. The filtered signal was digitized with a 12-bit analog-to-digital converter (RC-Electronics,

Santa Barbara, CA, Mod. ISC-16) and stored on the hard disk of the Compaq-386 computer.

The cuvette was filled with 200–300  $\mu\text{l}$  of a suspension of labeled membrane fragments (usually about 5  $\mu\text{g}$  protein per ml) in a medium containing 30 mM imidazole buffer, pH 7.2, and 1 mM EDTA.

### PHOTOCHEMICAL RELEASE OF ATP IN THE FLUORESCENCE CUVETTE

Light flashes (wavelength: 308 nm; total energy: 150 mJ; duration: 10 nsec) were generated with a EMG 100 excimer laser (Lambda Physics, Göttingen). At pH 7.0, ATP is liberated from "caged" ATP (cg-ATP) with a time constant of 4.6 msec (McCray et al., 1980). The concentration of released ATP was determined by the luciferin/luciferase test which was calibrated using solutions of known ATP concentration (De Luca & McElroy, 1978; Ernst, Böhme & Böger, 1983). If not otherwise stated, the concentration of cg-ATP was 100  $\mu\text{M}$ . About 15–25  $\mu\text{M}$  ATP were released in a single flash, corresponding to a photochemical yield of 15–25%.

Care had to be taken to avoid spatial inhomogeneities in the concentration of released ATP in the fluorescence cuvette, since concentration gradients of ATP can lead to distortions in the time course of the optical signal. Even if the light intensity is sufficiently constant over the cross section of the laser beam, intensity gradients in the direction of propagation may result from light absorption in the solution. At 308 nm, cg-ATP has an extinction coefficient of about 2000  $\text{M}^{-1} \text{cm}^{-1}$  (*unpublished data*). This means that the path length for an  $e$ -fold change of light intensity is 22 mm at a concentration of 100  $\mu\text{M}$ . When the height of the solution layer in the cuvette is 6 mm, a maximum intensity variation by a factor of 1.3 may be expected. Part of this intensity variation was eliminated by back reflection from the mirror at the bottom of the cuvette. Effects of concentration gradients of ATP may be estimated to be negligible in the experiments in which ATP binds to the high affinity site. Since the dissociation constant of ATP at the high affinity site is of the order of 0.1–1  $\mu\text{M}$ , the binding sites are almost completely saturated at a concentration of released ATP of 15–25  $\mu\text{M}$ , independent of small variations in the ATP concentration within the cuvette. In the experiments with sodium-free  $\text{K}^+$  solutions, in which ATP acts at a low-affinity site, errors introduced by distortion of the fluorescence signal have to be taken into account.

### RECORDING OF ELECTRICAL SIGNALS

Optically black films were formed from a solution of 10 mg/ml diphytanoylphosphatidylcholine in  $n$ -decane (Läuger et al., 1967; Borlinghaus et al., 1987). The membrane cell which was made of Teflon consisted of two compartments separated by a thin Teflon septum with a circular hole of 1.3 mm diameter. One compartment could be completely closed after filling with the aqueous solution; this increased the mechanical stability of the membrane and allowed efficient stirring in the open compartment (*cis* side) to which Na,K-ATPase membrane fragments were added (Fig. 2). The solution volumes of the closed and the open compartments were 5 and 0.3 ml, respectively. The Teflon cell was enclosed in a thermostated metal block with openings for the entry of the UV-light beam and for visual observation of the mem-

brane. The area of the black film was measured with an eye-piece micrometer.

The solutions on either side of the lipid membrane were connected to the external measuring circuit via agar bridges and silver/silver-chloride electrodes. In order to minimize stray-light artifacts from the electrodes, a suspension of carbon-black was added to the agar. For current measurements under short-circuit conditions, the signal was amplified with a Keithley Mod. 427 current amplifier, with the risetime usually set at 3 msec. For measuring voltage signals, a Mod. 3528 Burr-Brown amplifier with an input impedance of  $10^{12} \Omega$  was used. The signals were recorded with a digital oscilloscope (Nicolet Mod. 4094 A) and stored on diskettes. The membrane cell and the electrodes were enclosed in a Faraday shield.

If not otherwise indicated, the aqueous solutions contained 30 mM imidazole, pH 7.2, 10 mM  $\text{MgCl}_2$ , and various concentrations of NaCl and KCl. "Caged" ATP (usually 0.24 mM) and membrane fragments (about 40  $\mu\text{g}$  protein/ml) were added together to the open compartment (*cis* side) under stirring. The stirring was continued for about 1 min. Electrical signals were recorded 20–30 min after addition of membrane fragments to the cell.

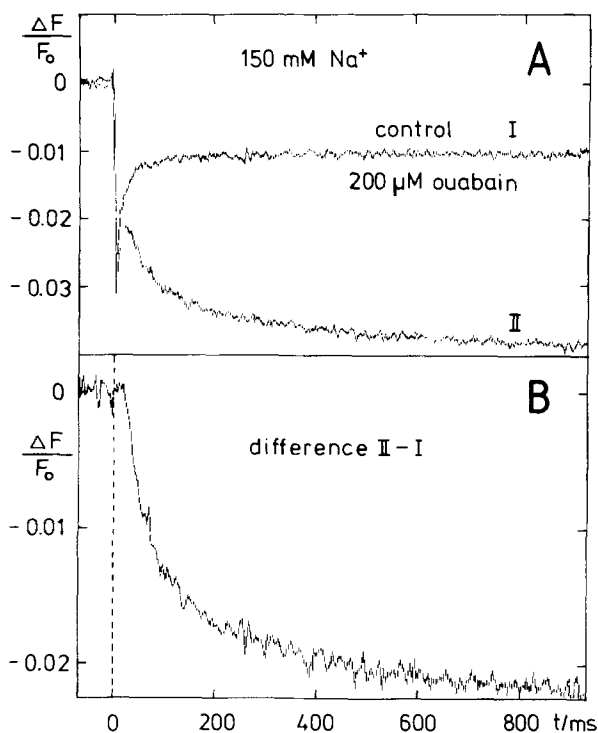
Light flashes of 40  $\mu\text{sec}$  duration and a total energy of 5 J were generated with a Xenon flash-tube (Mod. 5M-3) from EG&G Electro-Optics (Salem, MA). The emitted light passed through a bandpass filter with >50% transparency between 260 and 380 nm (Schott, Mainz, Mod. UG11). The light beam entered the cell from the *trans* side (Fig. 2) and was focussed onto the membrane.

## Results

### FLUORESCENCE SIGNALS IN THE PRESENCE OF $\text{Na}^+$

#### *Intrinsic Dye Response*

When a suspension of 5-IAF-labeled membrane fragments in  $\text{K}^+$ -free  $\text{Na}^+$  buffer was irradiated by a 308-nm laser flash in the presence of a blocking concentration (500  $\mu\text{M}$ ) of ouabain, a fast decrease of fluorescence intensity by 3–5% was observed, followed by a slow recovery to about 99% of the original level within 50 msec (Fig. 4A). Repetitive flashes led to a gradual bleaching of the fluorescent dye. A nearly identical flash-induced fluorescence signal was observed without ouabain, when either caged ATP or  $\text{Mg}^{2+}$  or  $\text{Na}^+$  were omitted from the solution. The origin of this intrinsic dye response is not clear so far; it may result from transient formation of an oxidized intermediate of the dye (Lindqvist, 1960). Degassing the solution only slightly reduced the amplitude of the signal. A similar bleaching artifact, but with faster recovery (within about 10 msec) was observed with a solution of 15 nM 5-IAF in buffer without membrane fragments (*not shown*).



**Fig. 4.** Relative fluorescence change  $\Delta F/F_0$  under  $K^+$ -free conditions as a function of time  $t$  after a 308-nm light-flash of 10 nsec duration given at time  $t = 0$ .  $F_0$  is the fluorescence intensity prior to the flash. Excitation wavelength: 481 nm; emission wavelength: 523 nm. The temperature was 20°C. (A) Suspension of 5-IAF-labeled membrane fragments (about 5  $\mu\text{g}$  protein/ml) in 30 mM imidazole, pH 7.2, 1 mM EDTA, 150 mM NaCl, 10 mM  $\text{MgCl}_2$  and 100  $\mu\text{M}$  caged ATP. In the control experiments (curve I), 500  $\mu\text{M}$  ouabain was added. The concentration of released ATP was estimated to be about 20  $\mu\text{M}$ . (B) difference II-I

#### Fluorescence Signals Associated with Pump Activity

For each set of experiments, a control experiment was carried out in which the time course of the intrinsic dye response described above was recorded under conditions under which pump activity was inhibited (Fig. 4A). Pump inhibition was achieved by adding a saturating concentration (500  $\mu\text{M}$ ) of ouabain, or (in the experiments with  $K^+$  media) by omitting  $\text{Mg}^{2+}$ . The control signal was stored and was subtracted from the fluorescence signals observed in the normal experiment (Fig. 4B).

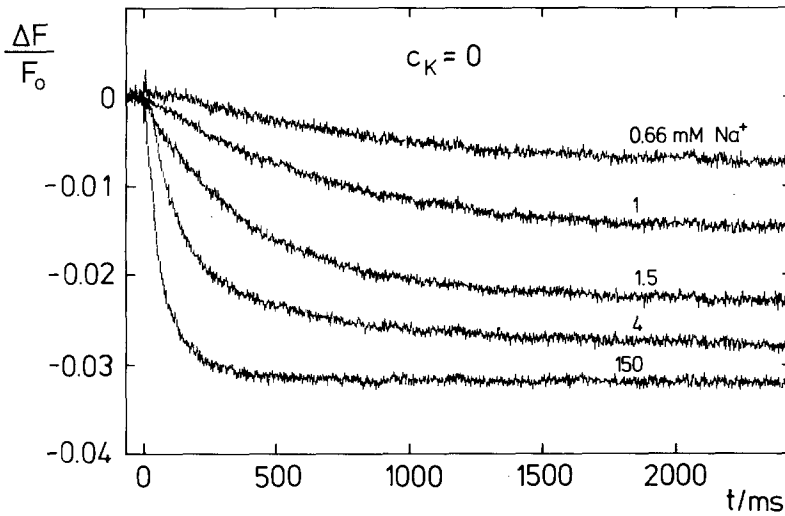
The difference signal in Fig. 4B exhibits a short lag phase followed by a nearly exponential decay with a time constant of  $\tau \approx 50$  msec. The observed drop of fluorescence after addition of ATP in the presence of  $\text{Na}^+$  and  $\text{Mg}^{2+}$  qualitatively agrees with previous findings of Kapakos and Steinberg

(1986b). The maximal fluorescence change,  $\Delta F(t \rightarrow \infty)/F_0$ , in our experiments with rabbit kidney enzyme is smaller than observed by Kapakos and Steinberg with dog enzyme (about 2–3% for rabbit enzyme at 5 mM  $\text{Na}^+$  compared to  $\approx 7\%$  for dog enzyme under similar conditions).

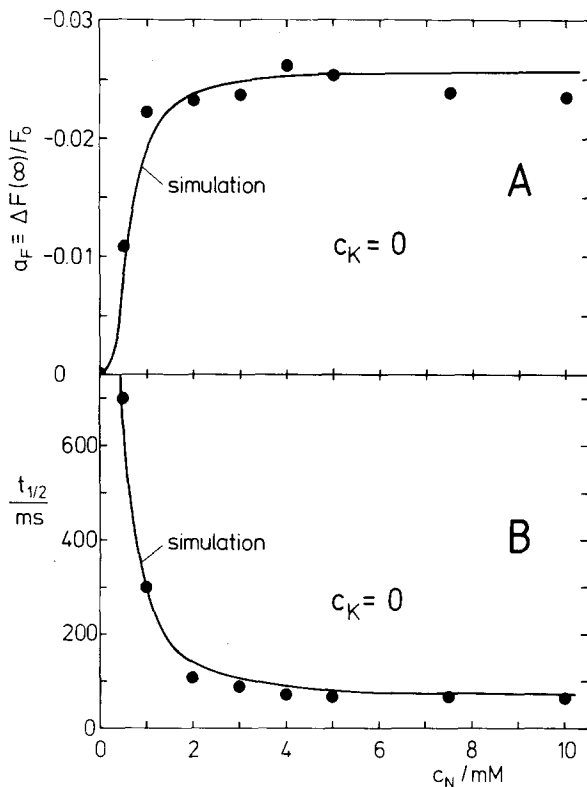
The lag phase of the fluorescence signal after the ATP concentration jump is likely to be determined by the finite rates of photochemical release and binding of ATP to the protein (Apell et al., 1987; Borlinghaus & Apell, 1988). The rate constant of release of ATP from caged ATP is about 140  $\text{sec}^{-1}$  at pH 7.2 and 22°C (McCray et al., 1980). Caged ATP is known to bind to the ATP site of Na,K-ATPase with an equilibrium dissociation constant estimated in the range of 30–500  $\mu\text{M}$  (Forbush, 1984; Nagel et al., 1987; Borlinghaus & Apell, 1988), whereas ATP binds to the  $E_1$  form of the enzyme with much higher affinity (dissociation constant 0.1–1  $\mu\text{M}$ ). Accordingly, ATP released in the aqueous solution has to compete with caged ATP bound to the ATP site of the enzyme. Furthermore, bound caged-ATP may be transformed into ATP in situ. It has been shown previously (Borlinghaus & Apell, 1988) by numerical simulation that the finite rate of the reactions preceding phosphorylation may be described by an effective time constant of ATP release and binding of about 20–50 msec under the experimental conditions of Fig. 4. This time constant approximately agrees with the observed lag time in Fig. 4B. However, because of the bleaching artifact, the exact shape of the intrinsic fluorescence signal is difficult to determine in the time range of 0–30 msec. Reliable information may be obtained from the decay of the fluorescence signal at times  $t > 30$  msec.

Previous studies indicate that phosphorylation by ATP in the absence of  $K^+$  leads to the reaction sequence  $\text{Na}_3 \cdot E_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)E_1-P \rightarrow P-E_2 \cdot \text{Na}_3 \rightarrow P-E_2$  (Glynn, 1985). Under  $K^+$ -free conditions,  $P-E_2$  is a long-lived state, which only slowly (with a rate constant  $r_f \approx 1-5 \text{ sec}^{-1}$ ) returns to state  $E_1$ . It is therefore likely to assume that the fluorescence decay in Fig. 4B reflects the  $E_1 \rightarrow E_2$  conformational transition of the protein (Kapakos & Steinberg, 1986a,b). This conclusion is consistent with the results of other fluorescence experiments using intrinsic and extrinsic probes (Karlsh & Yates, 1978; Jørgensen & Karlsh, 1980; Taniguchi et al., 1983; Glynn et al., 1987).

From direct measurements of the rates of phosphorylation and dephosphorylation (Mårdh & Zetterquist, 1974; Mårdh, 1975) it is known that the transition  $\text{Na}_3 \cdot E_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)E_1-P$  is much faster than the subsequent deocclusion step



**Fig. 5.** Relative fluorescence change  $\Delta F/F_0$  as a function of time  $t$  for different  $\text{Na}^+$  concentrations (0.66, 1, 1.5, 4 and 150 mM) and 5 mM  $\text{Mg}^{2+}$ . At time  $t = 0$ , about 20  $\mu\text{M}$  ATP were released in the solution. The other experimental conditions were the same as in Fig. 4

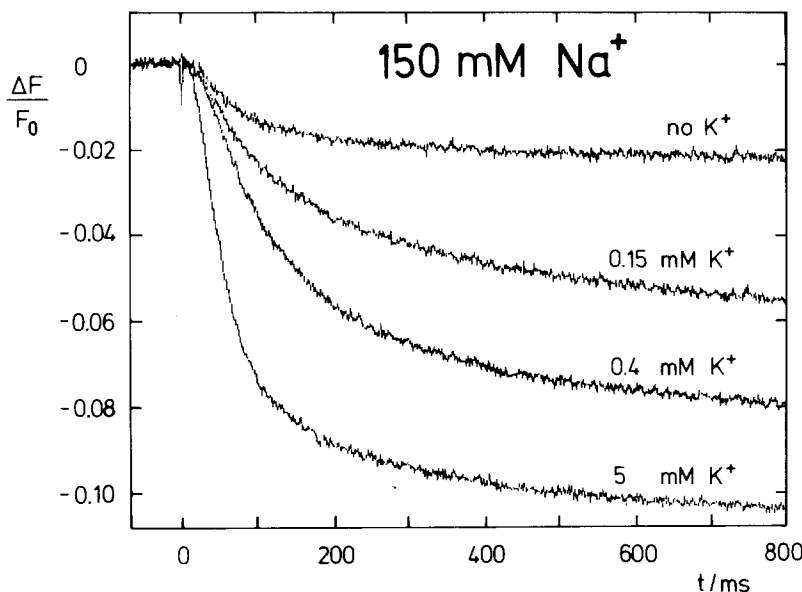


**Fig. 6.** Amplitude  $a_F \equiv \Delta F(\infty)/F_0$  and half-time  $t_{1/2}$  of the ATP-induced fluorescence decrease (Fig. 5) under  $\text{K}^+$ -free conditions as a function of  $\text{Na}^+$  concentration  $c_N$ .  $t_{1/2}$  is the time at which  $\Delta F/F_0$  reaches the half-maximal value  $a_F/2$ . Experimental data are represented by circles. The lines have been obtained by numerical simulation of the reaction cycle of Fig. 15, using the parameter values of the Table (see text).  $a_F$  was corrected for the intrinsic fluorescence change of the dye, as described in the legend of Fig. 4. The experimental conditions were the same as in the experiments of Fig. 5

$[(\text{Na}_3)\text{E}_1 \cdot \text{ATP} \rightarrow \text{P}-\text{E}_2 \cdot \text{Na}_3]$ . If the fluorescence of states  $\text{Na}_3 \cdot \text{E}_1 \cdot \text{ATP}$  and  $(\text{Na}_3)\text{E}_1-\text{P}$  is different, then a fast fluorescence change should precede the slow decay of the signal. Since such a fast component of the signal is not observed (Fig. 4B), it is likely to assume that states  $\text{Na}_3 \cdot \text{E}_1 \cdot \text{ATP}$  and  $(\text{Na}_3)\text{E}_1-\text{P}$  have similar fluorescence properties. The sensitivity by which fast fluorescence changes can be detected is limited, however, by the intrinsic dye response (Fig. 4A) and by the finite rate of the reactions preceding phosphorylation. More direct support for the assumption that the transition  $\text{Na}_3 \cdot \text{E}_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)\text{E}_1-\text{P}$  does not contribute to the fluorescence signal comes from experiments with chymotrypsin-modified enzyme (see below).

The time course of the ATP-induced fluorescence change  $\Delta F/F_0$  is shown in Fig. 5 for the different  $\text{Na}^+$  concentrations (0.66, 1, 1.5, 4 and 150 mM).  $\Delta F(t)/F_0$  can be approximately fitted by a single exponential function with a time constant depending on sodium concentration. Occasionally, fluorescence signals were observed in which the initial decay of  $\Delta F/F_0$  was followed by a slower decrease extending over the time range of 1–2 sec. These biphasic signals, which were obtained with a few Na,K-ATPase preparations under otherwise identical conditions, were not analyzed further.

The amplitude  $a_F \equiv \Delta F(\infty)/F_0$  and the half-time  $t_{1/2}$  of the fluorescence signal are plotted as functions of  $\text{Na}^+$  concentration  $c_N$  in Fig. 6.  $t_{1/2}$  is the time at which  $\Delta F/F_0$  reaches the half-maximal value  $a_F/2$ . As seen from Fig. 6B,  $t_{1/2}$  steeply decreases with increasing  $\text{Na}^+$  concentration. This has to be expected, since the rate of ATP-induced conformational change  $\text{E}_1 \rightarrow \text{E}_2$  is proportional to the concentration of  $\text{Na}_3 \cdot \text{E}_1$  which becomes small at low so-



**Fig. 7.** Relative fluorescence change  $\Delta F/F_0$  as a function of time  $t$  in the presence of  $\text{Na}^+$  and  $\text{K}^+$ . At time = 0 about  $20 \mu\text{M}$  ATP was photochemically released. The medium contained 5-IAF-labeled membrane fragments ( $5 \mu\text{g}$  protein/ml), 30 mM imidazole, 1 mM EDTA, pH 7.2,  $100 \mu\text{M}$  caged ATP, 5 mM  $\text{Mg}^{2+}$ , 150 mM NaCl, and various concentrations of KCl;  $T = 20^\circ\text{C}$ .  $\Delta F/F_0$  was corrected for the intrinsic fluorescence change of the dye

dium concentration. This explanation agrees with the results of numerical simulations of the reaction cycle (continuous line in Fig. 6B) to be discussed in detail later.

In the same  $\text{Na}^+$ -concentration range (0–3 mM) in which  $t_{1/2}$  decreases, the amplitude  $a_F$  of the signal increases towards a limiting value. This behavior, which has already been observed by Kapakos and Steinberg (1986b) in stationary experiments, results from the fact that at low  $\text{Na}^+$  concentration, release of ATP leads only to minor shift in the  $E_1/E_2$  concentration ratio due to spontaneous back reaction  $E_2 \rightarrow E_1$  (see below).

#### Chymotrypsin-Modified Enzyme

Treatment of Na,K-ATPase with  $\alpha$ -chymotrypsin in the presence of  $\text{Na}^+$  at low ionic strength leads to cleavage of a single peptide bond in the  $\alpha$ -subunit; the split is located in the cytoplasmic portion of the protein between Leu-266 and Ala-267 (Jørgensen & Collins, 1986). In the chymotrypsin-treated enzyme, phosphorylation by ATP, occlusion of  $\text{Na}^+$  and ADP/ATP exchange are preserved, while  $\text{Na}^+, \text{K}^+$  pumping and  $\text{Na}^+, \text{Na}^+$  exchange are abolished (Glynn, Hara & Richards, 1984; Jørgensen & Petersen, 1985). These findings indicate that modification by chymotrypsin stabilizes the enzyme in the  $E_1$  conformation by preventing the  $E_1 \rightarrow E_2$  transition.

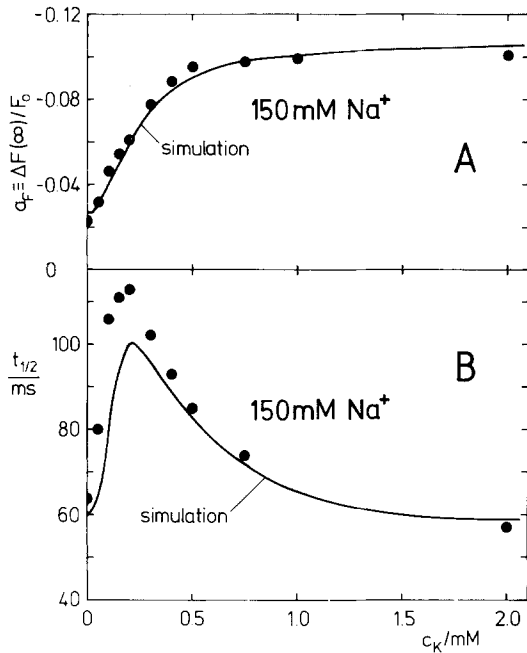
5-IAF-labeled membrane fragments (about 300  $\mu\text{g}/\text{ml}$ ) were incubated for 10–30 min at  $30^\circ\text{C}$  in a medium containing 10–20  $\mu\text{g}/\text{ml}$   $\alpha$ -chymotrypsin, 10 mM NaCl and 15 mM imidazole, pH 7.5 (Jørgen-

sen & Petersen, 1985). Under these conditions the proteolytic reaction may be expected to be selective, consisting in the cleavage of a single peptide bond, as mentioned above. After incubation, the membrane fragments were separated from the medium on a Sephadex G100 column. When the ATP-concentration jump experiment was done with the chymotrypsin-modified Na,K-ATPase under the conditions of Fig. 4, no fluorescence change was observed, apart from the intrinsic dye response. This finding agrees with recent observations from stopped-flow experiments with 5-IAF-labeled Na,K-ATPase (Steinberg & Karlish, 1989). In accordance with the results presented in the previous section, we may thus conclude that the transition  $\text{Na}_3 \cdot E_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)E_1 - P$  does not contribute to the fluorescence signal.

The most likely explanation of the experiment of Fig. 4B therefore consists in the assumption that the observed fluorescence decay results from the deocclusion step  $(\text{Na}_3)E_1 - P \rightarrow P - E_2 \cdot \text{Na}_3$ , followed by release of  $\text{Na}^+$  from the extracellular binding sites.

#### FLUORESCENCE SIGNALS IN PRESENCE OF $\text{Na}^+$ AND $\text{K}^+$

When, in the presence of a high concentration of  $\text{Na}^+$ , millimolar quantities of  $\text{K}^+$  are added to the medium, the amplitude of the ATP-induced signal strongly increases, while the time course of the fluorescence decay (at high sodium concentration) does not appreciably change (Fig. 7). The dependence of signal amplitude  $a_F$  and of half-time  $t_{1/2}$  on potas-



**Fig. 8.** Amplitude  $a_F = \Delta F(\infty)/F_0$  and half-time  $t_{1/2}$  of the ATP-induced fluorescence decrease in the presence of 150 mM  $\text{Na}^+$  as a function of  $\text{K}^+$  concentration  $c_K$ .  $t_{1/2}$  is the time at which  $\Delta F/F_0$  reaches the half-maximal value  $a_F/2$ . Experimental data are represented by circles. The lines have been obtained by numerical simulation of the reaction cycle of Fig. 15, using the parameter values of the Table (see text).  $a_F$  was corrected for the intrinsic fluorescence change of the dye, which was recorded in the absence of  $\text{Na}^+$  and  $\text{K}^+$ . Apart from  $c_K$ , the conditions were the same as in the experiments of Fig. 7

sium concentration  $c_K$  is shown in Fig. 8 together with the results of numerical simulations of the reaction cycle (full lines). The amplitude  $a_F$  exhibits a saturation behavior while the half-time  $t_{1/2}$  increases from about 60 msec towards a peak value of  $\approx 110$  msec and thereafter decreases again.

The effect of  $\text{K}^+$  on the ATP-induced fluorescence change may be explained in the following way. In the experiments represented in Figs. 7 and 8, the concentration of flash-released ATP ( $\approx 20 \mu\text{M}$ ) was much smaller than the dissociation constant of ATP at the low-affinity binding site, which is about 0.5 mM (Robinson & Flashner, 1979). Under this condition, phosphorylation of the enzyme mainly populates state  $E_2(\text{K}_2)$  via the reaction sequence  $P-E_2 \cdot \text{Na}_3 \rightarrow P-E_2 \cdot \text{K}_2 \rightarrow E_2(\text{K}_2)$ , since at low ATP concentration the transition  $E_2(\text{K}_2) \rightarrow \text{K}_2 \cdot E_1$  is extremely slow (Glynn, 1985). Accordingly, if state  $E_2(\text{K}_2)$  has a lower fluorescence than state  $P-E_2$  (Kapakos & Steinberg, 1986b), the total fluorescence decrease becomes larger when the protein is phosphorylated in the presence of  $\text{K}^+$ . The lack of a large effect of  $\text{K}^+$  on the time behavior of the

signal may be explained, assuming that the rate-limiting step in the reaction sequence  $E_1 \rightarrow \dots \rightarrow E_2(\text{K}_2)$  is the deocclusion of  $\text{Na}^+$ , both in the absence and in the presence of millimolar concentrations of  $\text{K}^+$ . This assumption is substantiated by numerical simulations of the reaction cycle, as will be discussed later.

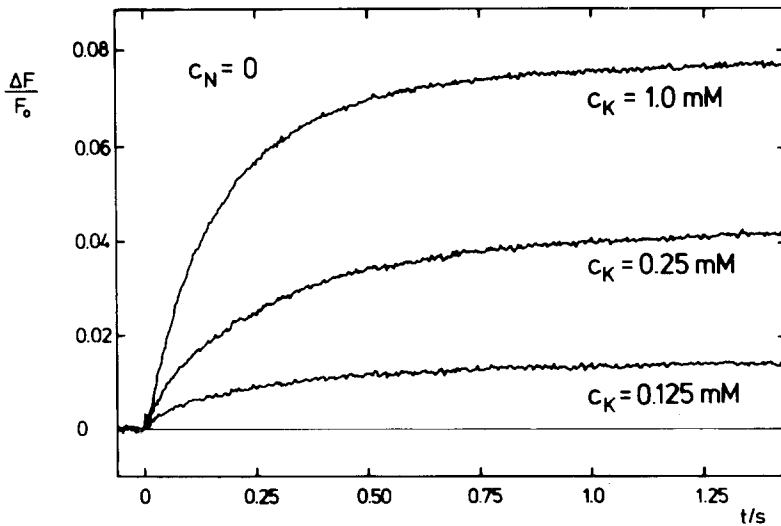
#### FLUORESCENCE SIGNALS IN THE PRESENCE OF $\text{K}^+$

When the medium contains  $\text{K}^+$ , but not  $\text{Na}^+$ , an ATP-concentration jump leads to a fluorescence increase, i.e., to a signal of opposite polarity compared to the signals observed with  $\text{Na}^+$  media (Fig. 9). For  $t > 20$  msec, the time course of the fluorescence change can be approximately described by a simple exponential relation of the form  $\Delta F/F_0 = a[1 - \exp(-t/\tau)]$ . In the absence of  $\text{Na}^+$ , ATP acts on the low-affinity nucleotide-binding site, so that at the given concentration of photochemically released ATP ( $\approx 20 \mu\text{M}$ ), the photoresponse remains far from saturation. This means that  $\Delta F(t)/F_0$  may be affected by inhomogeneities in ATP concentration resulting from spatial variations of laser-light intensity. For this reason the values of amplitude  $a_F$  and time constant  $\tau$  of the signal represent averages over a range of ATP concentrations.

As seen from Fig. 10, the signal amplitude  $a_F$  increases with increasing  $\text{K}^+$  concentration  $c_K$  up to a maximum and thereafter decreases again. The positive value of  $a_F$  is consistent with the assumption discussed in the previous section that  $E_2(\text{K}_2)$  has a lower fluorescence than  $E_1$ . In the presence of millimolar concentrations of  $\text{K}^+$  and in the absence of  $\text{Na}^+$  and ATP, a substantial fraction of the enzyme is initially present in state  $E_2(\text{K}_2)$ , since the equilibrium between  $\text{K}_2 \cdot E_1$  and  $E_2(\text{K}_2)$  is strongly poised (about 1000-fold) towards  $E_2(\text{K}_2)$  (Karlsh, 1980; Karlsh & Stein, 1982). Binding of ATP to  $E_2(\text{K}_2)$  shifts the equilibrium back to state  $E_1 \cdot \text{ATP}$ , which gives rise to an increase of fluorescence. In the presence of high concentrations of  $\text{K}^+$ , the enzyme remains mainly in states  $\text{K}_2 \cdot E_1 \cdot \text{ATP}$  and  $\text{ATP} \cdot E_2(\text{K}_2)/E_2(\text{K}_2)$  after ATP release, so that the fluorescence change is smaller. These predictions are consistent with the results of numerical simulations of the reaction cycle (continuous line in Fig. 10A).

The half-time  $t_{1/2}$  of the fluorescence signal  $\Delta F(t)/F_0$  decreases from 240 to 60 msec when the  $\text{K}^+$  concentration  $c_K$  increases from 0.25 to 10 mM (Fig. 10B).  $(\ln 2)/t_{1/2}$  may be assumed to correspond to the rate constant of the  $E_2 \rightarrow E_1$  transition, which, at  $c_K = 0.25$  mM, is about  $2.9 \text{ sec}^{-1}$  under our experimental conditions (concentration of re-





**Fig. 9.** Fluorescence signal  $\Delta F/F_0$  in a sodium-free potassium medium. At time  $t = 0$  about  $20 \mu\text{M}$  ATP were released in a solution containing 0.125, 0.25, or 1 mM  $\text{K}^+$ ;  $T = 20^\circ\text{C}$ .  $\Delta F/F_0$  was corrected for the intrinsic fluorescence change of the dye recorded in the absence of  $\text{Na}^+$  and  $\text{K}^+$ . The other experimental conditions were the same as in Fig. 7

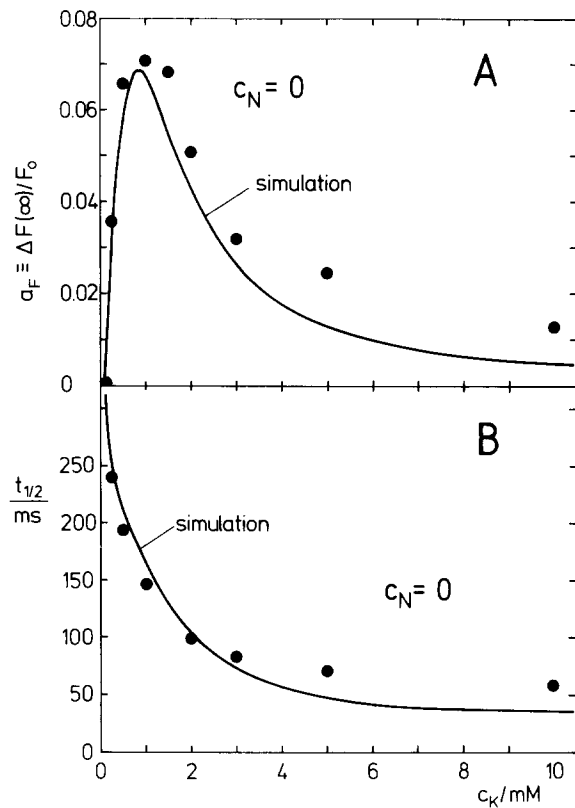
leased ATP about  $20 \mu\text{M}$ ). This value may be compared with the rate constant reported by Glynn et al. (1987) at  $5 \mu\text{M}$  ATP and  $0.1 \text{ mM}$   $\text{Rb}^+$  ( $0.57 \text{ sec}^{-1}$  at  $T = 20^\circ\text{C}$ ). At saturating ATP concentrations ( $c_T \gg 0.3 \text{ mM}$ ) Forbush (1987a) observed at  $20^\circ\text{C}$  a rate of  $\text{K}^+$  release of  $45 \text{ sec}^{-1}$ , representing a lower limit for the rate of the  $E_2 \rightarrow E_1$  transition at high ATP concentration.

The half-time  $t_{1/2}$ , as well as the amplitude  $a_F$  of the fluorescence signal were found to depend on the  $\text{Mg}^{2+}$  concentration.  $t_{1/2}$  increases about 1.7-fold and  $a_F$  about 1.4-fold when the  $\text{Mg}^{2+}$  concentration was increased from 5 to 10 mM.

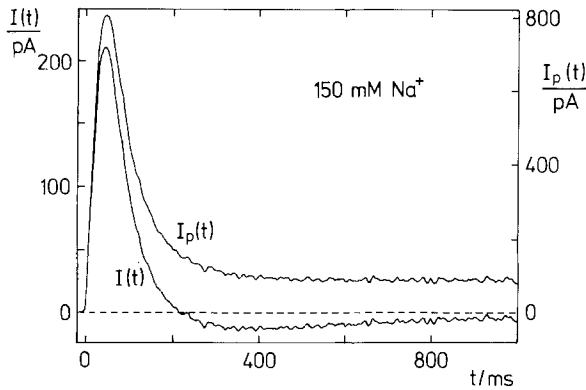
## TRANSIENT ELECTRIC CURRENTS

### *Electric Signals in the Presence of $\text{Na}^+$*

Membrane fragments labeled with 5-IAF were added together with  $240 \mu\text{M}$  caged ATP to one side of a planar lipid bilayer, as described under Materials and Methods. After a waiting time of 20–30 min, which is probably required for adsorption of membrane fragments, the photoresponse of the system was fully developed. A light pulse of  $40 \mu\text{sec}$  duration which liberated about  $25 \mu\text{M}$  ATP on the *cis* side of the bilayer (Fig. 2) elicited a transient electric current  $I$  (Fig. 11). In these experiments the planar lipid bilayer acts as a capacitive element which couples electrical events in the protein layer to the external measuring circuit (Borlinghaus et al., 1987). In the experiment represented in Fig. 11 the aqueous solutions contained  $\text{Na}^+$ , but no  $\text{K}^+$ . The sign of the early phase of the current corresponds to



**Fig. 10.** Amplitude  $a_F \equiv \Delta F(\infty)/F_0$  and half-time  $t_{1/2}$  of the ATP-induced fluorescence under sodium-free conditions, as a function of potassium concentration  $c_K$ .  $t_{1/2}$  is the time at which  $\Delta F/F_0$  reaches the half-maximal value  $a_F/2$ . The experimental conditions were the same as in the legend of Fig. 9. Experimental data are represented by circles. The lines have been obtained by numerical simulation of the reaction cycle of Fig. 15, using the parameter values of the Table (see text)



**Fig. 11.** Current signal  $I(t)$  in the absence of  $K^+$  from a lipid bilayer with bound Na,K-ATPase membrane fragments (Fig. 2). At time  $t = 0$ , about  $20 \mu\text{M}$  ATP was released from caged ATP by a 40- $\mu\text{sec}$  light flash.  $I(t)$  was computed from the recorded voltage signal  $V(t)$  according to  $I(t) = -AC_f dV/dt$ . The area  $A$  of the black film (specific capacitance  $C_f \approx 0.37 \mu\text{F}/\text{cm}^2$ ) was determined by an eye-piece micrometer ( $A \approx 0.60 \text{mm}^2$ ). The aqueous solutions contained 150 mM NaCl, 30 mM imidazole, pH 7.2, and 10 mM  $\text{MgCl}_2$ . The temperature was  $20^\circ\text{C}$ . Membrane fragments ( $40 \mu\text{g}/\text{ml}$ ) and  $240 \mu\text{M}$  "caged" ATP were added to the *cis* side (Fig. 2) 20 min prior to the experiment. The voltage signal was recorded at a bandwidth of 1 kHz. The intrinsic pump current  $I_p(t)$  was evaluated from  $I(t)$  according to Eq. (2) of Borlinghaus et al. (1987). The time constant  $\tau_v$  of the voltage decay at long times, which is required for the evaluation of  $I_p(t)$ , was determined to be 400 msec

a movement of positive charge from the solution toward the lipid bilayer. The transient current is generated by those membrane fragments that are bound to the bilayer with the cytoplasmic side facing the aqueous medium (Borlinghaus et al., 1987).

Charge translocation after activation of the pump can be detected either as a current  $I(t)$  under short-circuit conditions (Fig. 2), or as a voltage  $V(t)$ . It has been demonstrated previously (Borlinghaus et al., 1987) that voltage and current signals are strictly correlated according to the relation  $I(t) = -AC_f dV/dt$ , where  $A$  and  $C_f$  are the area and the specific capacitance of the lipid film, respectively. Since a measurement of  $V(t)$  yields a better signal-to-noise ratio, in most experiments voltage signals were recorded.  $V(t)$  was subsequently converted into a current  $I(t)$  by numerical differentiation. The scaling factor  $AC_f$  was estimated by determining the area of the black film with an eye-piece micrometer, using a value of  $C_f \approx 0.37 \mu\text{F}/\text{cm}^2$  for the specific capacitance (Borlinghaus et al., 1987). Since the absolute magnitude of the current is not used in the subsequent analysis of the electrical signals, errors in the determination of the scaling factor may be neglected.

From the current signal in the external measur-

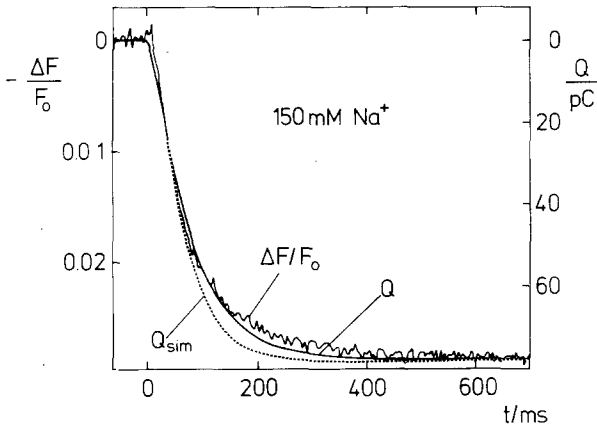
ing circuit,  $I(t)$ , the intrinsic pump current  $I_p(t)$  can be evaluated.  $I_p(t)$  is the current that would be observed in a fictitious experiment in which a continuous layer of membrane fragments is directly interposed (without supporting bilayer) between the aqueous solutions.  $I_p(t)$  and  $I(t)$  are connected by the circuit parameters of the compound membrane system which may be estimated from the shape of  $V(t)$  at long times (Borlinghaus et al., 1987). From Fig. 11 it is seen that  $I_p(t)$  and  $I(t)$  differ only at large values of  $t$ . In particular, the negative phase of  $I(t)$  which results from backflow of charge across the shunt conductance of the membrane fragments is not present in  $I_p(t)$ . Instead,  $I_p(t)$  approaches a small quasistationary current  $I_p^\infty$  at long times which results from pump molecules undergoing the transition  $P-E_2 \rightarrow E_1$  and reentering the cycle again (Apell et al., 1987). The small amplitude of  $I_p^\infty$  is consistent with the observation that the rate of the transition  $P-E_2 \rightarrow E_1$  is extremely low ( $1-5 \text{sec}^{-1}$  at  $20^\circ\text{C}$ ) in the absence of  $K^+$  (Glynn & Karlish, 1976).

In order to test whether labeling of the protein with 5-IAF has any influence on the kinetics of charge translocation, parallel experiments were carried out with unlabeled membrane fragments. Within the experimental error limits, no difference in the shape of the current transient could be detected between labeled and unlabeled membrane preparations. This finding is consistent with the observation that labeling of Na,K-ATPase with 5-IAF does not affect the enzymatic activity (Kapakos & Steinberg, 1982).

#### COMPARISON OF ELECTRICAL AND OPTICAL SIGNALS ( $\text{Na}^+$ MEDIA)

Previous studies with chymotrypsin-modified enzyme (Borlinghaus et al., 1987) led to the conclusion that the major charge-carrying step in the sodium limb of the transport cycle is the deocclusion reaction  $(\text{Na}_3)E_1-P \rightarrow P-E_2 \cdot \text{Na}_3$ , followed by release of  $\text{Na}^+$  to the extracellular medium. In an analogous way, the optical experiments with chymotrypsin-treated protein described above indicate that the main fluorescence change after ATP-induced phosphorylation of the protein is associated with the same reaction sequence  $(\text{Na}_3)E_1-P \rightarrow P-E_2 \cdot \text{Na}_3$ .

The simplest situation for a comparison of optical and electrical signals is given when both the fluorescence change and the transient current result from a single reaction step  $A \rightarrow B$ . The fluorescence intensity  $F$  may then be represented by  $F = f_A c_A + f_B c_B$ , where  $f_A$  and  $f_B$  are the contributions of  $A$  and



**Fig. 12.** Comparison of ATP-induced electrical and optical signals measured in parallel experiments under nearly identical conditions (150 mM Na<sup>+</sup>, 30 mM imidazole, pH = 7.2, 1 mM EDTA, 10 mM Mg<sup>2+</sup>,  $T = 21\text{--}22^\circ\text{C}$ ).  $\Delta F/F_0$  is the relative fluorescence change and  $Q$  the translocated charge (Eq. (3));  $1 \text{ pC} \equiv 10^{-12}$  coulomb.  $Q_{\text{sim}}$  is the predicted value of the translocated charge, as obtained by numerical simulation of the reaction cycle of Fig. 15 with the parameter values of the Table, together with  $c_p = c_D = c_K = 0$  and with the following assignments of the dielectric coefficients:  $\alpha' = \alpha'' = \alpha_l = \alpha_r = 0$ ,  $\alpha_p = 1$  (see text). In the fluorescent experiment the concentration of caged ATP was 100  $\mu\text{M}$  and the concentration of released ATP was approximately 20  $\mu\text{M}$ . In the current measurement the concentration of caged ATP was 240  $\mu\text{M}$  and the concentration of released ATP about 30  $\mu\text{M}$

$B$  to  $F$ , and  $c_A$  and  $c_B$  are the concentrations. Introducing the initial fluorescence  $F_0 = f_{AC}$ , where  $c = c_A + c_B$  is the total concentration, the time course of the relative fluorescence change  $\Delta F/F_0 \equiv (F - F_0)/F_0$  is obtained as

$$\frac{\Delta F(t)}{F_0} = \frac{1}{c} \left( \frac{f_B}{f_A} - 1 \right) c_B(t). \quad (1)$$

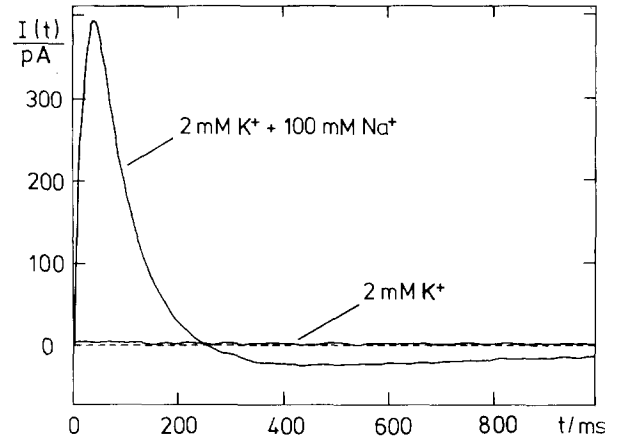
On the other hand, the transient pump current  $I_p(t) - I_p^\infty$  associated with the reaction  $A \rightarrow B$  may be written as

$$I_p(t) - I_p^\infty = ae_0 \frac{dc_B}{dt} \quad (2)$$

where  $e_0$  is the elementary charge and  $a$  is a constant;  $I_p^\infty$  accounts for any quasistationary component of  $I_p(t)$ . According to Eq. (2), the total translocated charge  $Q(t)$  is given by

$$Q(t) \equiv \int_0^t (I_p - I_p^\infty) = ae_0 c_B(t). \quad (3)$$

Comparison with Eq. (1) shows that under the assumptions introduced above,  $\Delta F(t)/F_0$  and  $Q(t)$



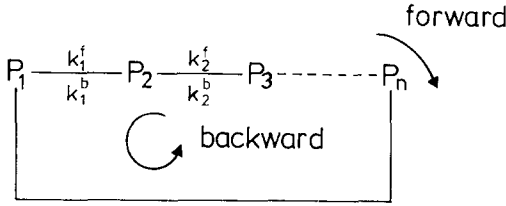
**Fig. 13.** Electrical transients in the presence of 2 mM K<sup>+</sup> alone and after addition of 100 mM Na<sup>+</sup>. The transient was measured as a voltage signal and was subsequently transformed into a current  $I(t)$  by digital differentiation.  $T = 25.5^\circ\text{C}$ . The other experimental conditions were the same as in Fig. 11

should exhibit the same time course, apart from a scaling factor.

A behavior predicted by Eqs. (1) and (3) is observed in experiments in K<sup>+</sup>-free Na<sup>+</sup> media. This is shown in Fig. 12 in which  $\Delta F(t)/F_0$  is plotted together with the translocated charge  $Q(t)$  for  $c_N = 150 \text{ mM}$ .  $Q(t)$  was obtained according to Eq. (3) as the time integral of  $I_p - I_p^\infty$ . It is seen that  $\Delta F(t)/F_0$  and  $Q(t)$  nearly coincide. This indicates that both the fluorescence change as well as the charge translocation take place in the same reaction step. As discussed above, a likely candidate for this common reaction step is the deocclusion of sodium.

#### Electrical Signals in the Presence of K<sup>+</sup>

When the medium contained 2 mM K<sup>+</sup>, but no Na<sup>+</sup>, the transient electric current following an ATP-concentration jump was virtually zero (Fig. 13). As seen from Fig. 13, subsequent addition of 100 mM Na<sup>+</sup> and photochemical ATP release gave rise to a large current signal. Similar results were obtained when the K<sup>+</sup> concentration was varied in the range between 1 and 10 mM. In some experiments, at high amplification, a small current signal could be detected in the presence of K<sup>+</sup> alone, exhibiting a biphasic shape with a peak at  $t \approx 0\text{--}100$  msec and a subsequent decline to zero. The signal was always positive (corresponding to translocation of positive charge towards the lipid bilayer), but the amplitude was subjected to considerable variations from experiment to experiment. It cannot be excluded that the spurious currents observed in K<sup>+</sup> media were caused by trace impurities of Na<sup>+</sup>. As discussed



**Fig. 14.** Transitions between states  $P_1, P_2, \dots, P_n$  of a pump molecule.  $k_1^f, k_2^f, \dots$  and  $k_1^b, k_2^b, \dots$  are rate constants for transitions in forward and backward direction, respectively

previously (Läuger & Apell, 1986), intrinsic charge translocations other than movements of binding sites can contribute to the current signal. From the current transient under nominally  $\text{Na}^+$ -free conditions, the total translocated charge  $Q$  could be approximately determined. For this purpose the measured current  $I(t)$  was transformed into the intrinsic pump current  $I_p(t)$  as described above. The charge  $Q_\infty$  was obtained from the time integral of  $I_p(t) - I_p^\infty$  between the limits  $t = 0$  and  $t \rightarrow \infty$ . From a series of experiments of the kind represented in Fig. 13, the ratio  $\rho$  of translocated charge in the absence and in the presence of  $\text{Na}^+$  was determined. The upper limit of  $\rho \equiv Q_\infty(K)/Q_\infty(K + \text{Na})$  was found to be approximately 0.01.

It is pertinent to note that the absence of a current transient under  $\text{Na}^+$ -free conditions is unlikely to be an artifact resulting from the inaccessibility of the extracellular side of the pump molecule facing the lipid bilayer. From previous studies (Glynn, 1985) it is known that in  $\text{Na}^+$ -free  $\text{K}^+$  media, the Na,K-ATPase is present in the form  $E_2(\text{K}_2)$  with occluded potassium (Fig. 1).

The transient currents represented in Figs. 11 and 13 are observed under single-turnover conditions in which the pump moves through part of the reaction cycle. From the  $\text{Na}^+$  experiment (Fig. 11), it is clear that the sensitivity of the current measurement is sufficient to detect charge translocation under single-turnover conditions, and therefore a current signal should have been observed in the  $\text{K}^+$  experiment (Fig. 13), if the transitions  $E_2(\text{K}_2) \rightarrow \text{K}_2 \cdot E_1 \rightarrow E_1$  are associated with charge movement. In the optical experiment which was carried out under virtually identical conditions, a large fluorescence change was observed after the light flash (Fig. 9), indicating that an appreciable shift of the conformation equilibrium between  $E_2(\text{K}_2)$  and  $\text{K}_2 \cdot E_1$  occurs after ATP release. Comparison of the optical and electrical signals thus leads to the conclusion that the transition  $\text{ATP} \cdot E_2(\text{K}_2) \rightarrow \text{K}_2 \cdot E_1 \cdot \text{ATP}$  is electrically silent.

## COMPARISON OF THE EXPERIMENTAL RESULTS WITH THEORETICAL PREDICTIONS

In the following we compare the experimental results with predictions derived from the Post-Albers reaction scheme. For this purpose, a numerical simulation of the transport cycle of Fig. 15 is carried out. The shape of the observed optical and electrical transients is found to agree with predictions from the reaction model, when the parameters of the model are chosen in an appropriate way.

### Time Dependence of Fluorescence Signal $\Delta F/F_0$ and Pump Current $I_p$

The method for evaluating the time behavior of  $\Delta F/F_0$  and  $I_p$  may be described on the basis of the general reaction scheme of Fig. 14 in which it is assumed that operation of the pump involves a sequence of transitions between states  $P_i$  ( $i = 1, 2, \dots, n$ ). The rate constants  $k_i^f$  and  $k_i^b$  in forward and backward direction are, in general, pseudomonomolecular rate constants which may contain concentrations, such as ion or nucleotide concentrations. The kinetic behavior of the system may be described by introducing the fraction  $x_i(t)$  of pump molecules in state  $P_i$  at time  $t$ . The time derivative of  $x_i$  is given by

$$dx_i/dt = -(k_{i-1}^b + k_i^f)x_i + k_{i-1}^f x_{i-1} + k_{i+1}^b x_{i+1}. \quad (4)$$

The  $n$  functions  $x_i(t)$  are obtained by numerical integration of the  $n$  relations given by Eq. (4). If  $N$  is the number of pump molecules contributing to the fluorescence signal and  $\varphi_i$  is the fluorescence contribution of a single pump molecule in state  $P_i$ , the measured fluorescence intensity  $F$  (corrected for background radiation) may be represented by

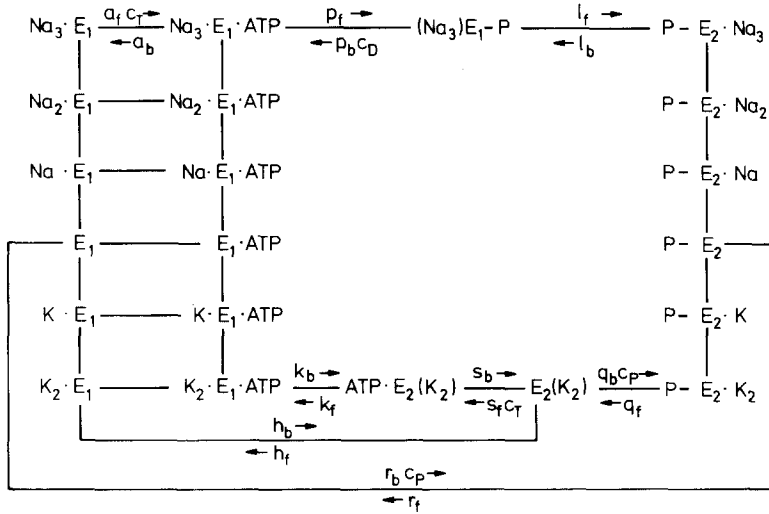
$$F = N \sum_i \varphi_i x_i. \quad (5)$$

Introducing the initial values  $x_{i0} \equiv x_i(0)$  of the quantities  $x_i$  (prior to the release of ATP) and the initial value  $F_0$  of  $F$ , the relative change of fluorescence intensity,  $\Delta F/F_0 \equiv (F - F_0)/F_0$ , is obtained as

$$\frac{\Delta F}{F_0} = \frac{\sum_i f_i (x_i - x_{i0})}{1 + \sum_i f_i x_{i0}} \quad (6)$$

$$f_i \equiv (\varphi_i - \varphi_1)/\varphi_1. \quad (7)$$

The quantities  $f_i$  are the relative fluorescence increments of state  $i$  with respect to state 1.



**Fig. 15.** Expanded form of the Post-Albers cycle (Fig. 1) for the evaluation of the time dependence of  $\Delta F/F_0$  and of  $I_p$ .  $a_f, p_f, \dots$  and  $a_b, p_b, \dots$  are rate constants for transitions in forward and backward direction, respectively.  $c_T, c_D$  and  $c_P$  are the concentrations of ATP, ADP and  $P_i$ . The rate constants  $a_f$  and  $a_b$  are assumed to be the same for all transitions  $Na_i \cdot E_1 \leftrightarrow Na_i \cdot E_1 \cdot ATP$  and  $K_j \cdot E_1 \leftrightarrow K_j \cdot E_1 \cdot ATP$  ( $i = 0, 1, 2, 3; j = 1, 2$ )

In order to describe the time dependence of the transient pump current  $I_p$ , we introduce the net rate  $\Phi_i$  of transitions  $P_i \rightarrow P_{i+1}$  (referred to a single pump molecule):

$$\Phi_i = k_i^f x_i - k_{i+1}^b x_{i+1}. \quad (8)$$

The contribution of  $\Phi_i$  to  $I_p$  may be written as  $e_0 N \alpha_i \Phi_i$ , where  $e_0$  is the elementary charge and  $\alpha_i$  the "dielectric coefficient" associated with transition  $P_i \rightarrow P_{i+1}$  (Läuger et al., 1981). This yields

$$I_p = e_0 N \sum_i \alpha_i \Phi_i. \quad (9)$$

The essential microscopic information provided by  $I_p(t)$  is contained in the dielectric coefficients  $\alpha_i$  which depend on the magnitude of the translocated charge and on the distance over which the charge moves.

It should be noted that the validity of Eqs. (6) and (9) is not restricted to the simple reaction cycle of Fig. 14. It is easily seen that Eqs. (6) and (9) also apply to arbitrarily branched reaction schemes.

### Reaction Model

The numerical analysis of Eqs. (6) and (9), which will be described below, is based on the Post-Albers cycle (Fig. 1) which is represented in more detailed form in Fig. 15. The reaction scheme of Fig. 15 is somewhat simplified insofar as additional phosphorylated states that have been postulated in the literature (Nørby, Klodos & Christiansen, 1983; Yoda & Yoda, 1986, 1987; Plesner & Plesner, 1988)

are omitted. Furthermore, Fig. 15 does not explicitly account for transitions between the unliganded states  $E_1$  and  $E_2$ . This seems justified, since the equilibrium between  $E_1$  and  $E_2$  lies far on the side of  $E_1$  (Karlisch & Stein, 1982). For the analysis of the reaction scheme we assume that ion-binding and -release steps are not rate-limiting and that  $Na^+$  and ATP (as well as  $K^+$  and ATP) bind independently to form  $E_1$  of the protein (Karlisch, Yates & Glynn, 1978a). This means that the following equilibrium relations hold at all times:

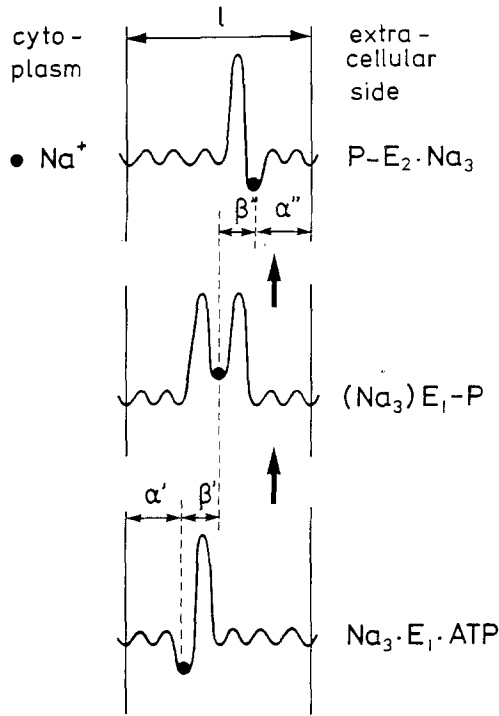
$$\frac{x[Na_i \cdot E_1]}{x[Na_{i-1} \cdot E_1]} = \frac{x[Na_i \cdot E_1 \cdot ATP]}{x[Na_{i-1} \cdot E_1 \cdot ATP]} = \frac{c_N}{K'_{Ni}} \equiv n'_i \quad (10)$$

$$\frac{x[K_j \cdot E_1]}{x[K_{j-1} \cdot E_1]} = \frac{x[K_j \cdot E_1 \cdot ATP]}{x[K_{j-1} \cdot E_1 \cdot ATP]} = \frac{c_K}{K'_{Kj}} \equiv k'_j \quad (11)$$

( $i = 1, 2, 3; j = 1, 2$ ).

$x[A]$  denotes the fraction of pump molecules in state  $A$ .  $c_N$  and  $c_K$  are the concentrations of  $Na^+$  and  $K^+$ , respectively, and  $K'_{Ni}$  and  $K'_{Kj}$  are equilibrium dissociation constants. Analogous equations hold for state  $P-E_2$ . The assumption of rapid binding and release of alkali ions has been introduced here to simplify the analysis. In view of recent experimental findings indicating that  $K^+$  release from state  $P-E_2 \cdot K_2$  may be slow (Forbush, 1987b), the equilibrium assumption should be replaced by a more realistic treatment as soon as more detailed kinetic information becomes available.

According to the principle of detailed balance, the rate constants and equilibrium constants are connected by the following relations, which correspond to three independent cycles in the reaction scheme of Fig. 15 (Läuger & Apell, 1986):



**Fig. 16.** Hypothetical energy profile of a sodium ion along the transport pathway. The ion binding sites in state  $\text{Na}_3 \cdot E_1 \cdot \text{ATP}$  are connected with the cytoplasmic side by a series of low barriers, but separated from the extracellular medium by a high barrier. In the “occluded” state  $(\text{Na}_3)E_1\text{-P}$  the energy barriers on either side are high. In state  $\text{P-E}_2 \cdot \text{Na}_3$  the binding sites are easily accessible from the extracellular phase.  $\alpha'$ ,  $\alpha''$ ,  $\beta'$ , and  $\beta''$  are dielectric distances, depending on the location of the ion binding site in the protein and on the dielectric properties of the protein and the surrounding medium

$$\frac{a_f k_b s_b h_f}{a_b k_f s_f h_b} = 1 \quad (12)$$

$$\frac{r_f q_b h_b}{r_b q_f h_f} \cdot \frac{K''_{K1} K''_{K2}}{K'_{K1} K'_{K2}} = 1 \quad (13)$$

$$\frac{p_f r_f a_f}{p_b l_b r_b a_b} \cdot \frac{K''_{N1} K''_{N2} K''_{N3}}{K'_{N1} K'_{N2} K'_{N3}} = K. \quad (14)$$

$K \equiv \bar{c}_D \bar{c}_P / \bar{c}_T$  is the equilibrium constant of ATP hydrolysis ( $\bar{c}_T$ ,  $\bar{c}_D$  and  $\bar{c}_P$  are equilibrium concentrations of ATP, ADP and  $P_i$ ).

For the calculation of  $\Delta F(t)/F_0$ , the rate equations [Eq. (4)] are integrated under the initial condition  $[\text{ATP}] \equiv c_T = 0$ , as described in Appendix A. The time course of  $c_T$  after the light flash at  $t = 0$  is assumed to be given by

$$c_T(t) = c_T^\infty [1 - \exp(-k_T t)]. \quad (15)$$

The quantity  $k_T$  represents an overall rate constant accounting for the release of ATP from caged ATP,

as well as for the exchange of caged ATP for ATP at the nucleotide binding site of the protein (Forbush, 1984). For a more detailed analysis of the reactions preceding binding of ATP, see Apell et al. (1987).

#### Evaluation of $I_p(t)$

To calculate  $I_p(t)$  from Eq. (9), the previously-described method for the evaluation of the net rates  $\Phi_i$  may be used (Apell et al., 1987). The analysis is based on the following assumptions:

a) Binding and release of ATP is treated as electrically silent processes. This means that the dielectric coefficients of the processes  $\text{Na}_i \cdot E_1 \rightarrow \text{Na}_i \cdot E_1 \cdot \text{ATP}$ ,  $\dots$ ,  $\text{K}_j \cdot E_1 \rightarrow \text{K}_j \cdot E_1 \cdot \text{ATP}$  and  $E_2(\text{K}_2) \rightarrow \text{ATP} \cdot E_2(\text{K}_2)$  are equal to zero.

b) The sodium binding sites and the potassium binding sites in state  $E_1$  (and also in state  $E_2$ ) are assumed to be electrically equivalent. Accordingly, the reactions  $\text{Na}_{i-1} \cdot E_1 \rightarrow \text{Na}_i \cdot E_1$  ( $i = 1, 2, 3$ ) and  $\text{K}_{j-1} \cdot E_1 \rightarrow \text{K}_j \cdot E_1$  ( $j = 1, 2$ ) are described by the same dielectric coefficient  $a'$ , which accounts for the depth of the “ion well” (Mitchell & Moyle, 1974) at the cytoplasmic side (Fig. 16). In a similar way, ion binding at the extracellular side is described by a dielectric coefficient  $\alpha''$ .

c) Intrinsic charge displacements in the protein (other than movements of the ion-binding sites) are neglected. This means that the dielectric coefficients corresponding to the reactions described by rate constants  $p$ ,  $l$ ,  $k$  and  $q$  in Fig. 15 given by

$$\alpha_p = (3 + z_L)\beta' \quad (16)$$

$$\alpha_l = (3 + z_L)\beta'' \quad (17)$$

$$\alpha_k = (2 + z_L)\gamma' \quad (18)$$

$$\alpha_q = (2 + z_L)\gamma''. \quad (19)$$

$z_L e_o$  is the charge of the empty ion-binding site, and  $\beta'$ ,  $\beta''$ ,  $\gamma'$ ,  $\gamma''$  are relative dielectric displacements as indicated in Fig. 16 ( $\gamma'$  and  $\gamma''$  are defined in an analogous way as  $\beta'$  and  $\beta''$ ). The quantities  $\alpha'$ ,  $\alpha''$ ,  $\dots$  are connected by the following relations (compare Fig. 16):

$$\alpha' + \alpha'' + \beta' + \beta'' = 1 \quad (20)$$

$$\alpha' + \alpha'' - \gamma' - \gamma'' = 1. \quad (21)$$

Since, according to assumption a), the coefficients  $\alpha_a$  and  $\alpha_s$  vanish,  $\alpha_h$  and  $\alpha_r$  are simply given by (compare Fig. 15):

$$\alpha_h = \alpha_k; \alpha_r = \alpha_q + \alpha_k. \quad (22)$$

**Table.** Values of kinetic parameters of the reaction scheme of Fig. 15, used for numerical simulation of  $\Delta F(t)/F_0$  and  $I_p(t)$ ;  $T = 20^\circ\text{C}$

| Parameter | Value   | Notes               |
|-----------|---|---------------------|
| $K'_N$    | 3 mM  | See text            |
| $K''_N$   | 200 mM  | See text            |
| $K'_K$    | 20 mM   | See text            |
| $K''_K$   | 1 mM  | See text            |
| $K$       | $4 \times 10^5 \text{ M}$                         | a                   |
| $p_f$     | $180 \text{ sec}^{-1}$                            | b                   |
| $p_b$     | $2 \times 10^4 \text{ M}^{-1} \text{ sec}^{-1}$   | c                   |
| $l_f$     | $19 \text{ sec}^{-1}$                             | d                   |
| $l_b$     | $1.7 \text{ sec}^{-1}$                            | d                   |
| $q_f$     | $500 \text{ sec}^{-1}$                            | e                   |
| $q_b$     | $5.8 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ | e                   |
| $s_f$     | $2.5 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ | f                   |
| $s_b$     | $140 \text{ sec}^{-1}$                            | f                   |
| $k_f$     | $15 \text{ sec}^{-1}$                             | g                   |
| $k_b$     | $670 \text{ sec}^{-1}$                            | h                   |
| $a_f$     | $10^7 \text{ M}^{-1} \text{ sec}^{-1}$            | i                   |
| $a_b$     | $20 \text{ sec}^{-1}$                             | Mårdh & Post (1977) |
| $r_f$     | $1 \text{ sec}^{-1}$                              | k                   |
| $r_b$     | $3.6 \times 10^4 \text{ M}^{-1} \text{ sec}^{-1}$ | l                   |
| $h_f$     | $0.2 \text{ sec}^{-1}$                            | m                   |
| $h_b$     | $250 \text{ sec}^{-1}$                            | m                   |

<sup>a</sup> Veech et al. (1979) give a value of  $\Delta G_0 = -32.4 \text{ kJ/mol}$  for the hydrolysis of ATP at pH 7.2, 1 mM  $\text{Mg}^{2+}$  and  $38^\circ\text{C}$ , corresponding to  $K = 2.8 \times 10^5 \text{ M}$ . With  $\Delta H = -25 \text{ kJ/mol}$  (Alberty, 1969),  $K$  becomes equal to  $4.2 \times 10^5 \text{ M}$  at  $20^\circ\text{C}$ .

<sup>b</sup> Mårdh and Zetterquist (1974) obtained, at  $21^\circ\text{C}$ , a value of  $180 \text{ sec}^{-1}$  for the pseudo-first-order rate constant of phosphorylation of bovine brain microsomal Na,K-ATPase when neither  $\text{Na}^+$  nor ATP were rate limiting.

<sup>c</sup> Estimated from Mårdh (1975); compare Läger & Apell, 1986.

<sup>d</sup>  $l_f$  and  $l_b$  were estimated by fitting Eq. (6) to the observed time course of  $\Delta F/F_0$ . For bovine-brain enzyme, Mårdh (1975) obtained a value of  $l_f \approx 80 \text{ sec}^{-1}$  at  $21^\circ\text{C}$ . The values of  $l_f$  and  $l_b$  of the Table approximately agree with the previous finding  $l_f/l_b \approx 10$  (Mårdh, 1975; Glynn, 1984).

<sup>e</sup>  $q_f/q_b$  was calculated from Eq. (13) to be 0.086 mM, using the numerical values of  $r_f, r_b, \dots$  given in this Table.  $q_f$  was arbitrarily chosen to be  $500 \text{ sec}^{-1}$ , assuming that the reaction  $P - E_2 \cdot K \rightarrow E_2(K_2)$  is not rate limiting; from deocclusion experiments, Forbush (1988) concluded that  $q_f$  is much larger than  $100 \text{ sec}^{-1}$  at pH 7.0. From  $q_f/q_b = 0.086 \text{ mM}$  and  $q_f = 500 \text{ sec}^{-1}$ ,  $q_b = 5.8 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$  is obtained.

<sup>f</sup> The value of  $s_f$  was arbitrarily chosen to be  $2.5 \times 10^6 \text{ M}^{-1} \text{ sec}^{-1}$ , assuming that ATP binding to  $E_2(K_2)$  is not rate limiting at millimolar ATP concentrations. With  $s_b = 140 \text{ sec}^{-1}$ , the ratio  $s_b/s_f$  becomes  $56 \mu\text{M}$ . This is smaller than estimated values of 0.1–1 mM for the equilibrium dissociation constant of ATP at the low-affinity site (Robinson & Flashner, 1979; Moczydlowski & Fortes, 1981).

<sup>g</sup> From time-resolved fluorescence experiments, Karlish and Yates (1978) estimated for the transition  $\text{ATP} \cdot E_2(K_2) \rightarrow K_2 \cdot E_2 \cdot \text{ATP}$  a rate of  $50 \text{ sec}^{-1}$  at  $20^\circ\text{C}$ . This value agrees with the rate of deocclusion of  $\text{K}^+$  ( $45 \text{ sec}^{-1}$  at  $20^\circ\text{C}$ ) observed by Forbush (1987a) at saturating ATP concentration.

<sup>h</sup> Calculated from Eq. (12), using the numerical values of  $a_f, a_b, \dots$  given in this Table. Karlish and Yates (1978) observed a value of  $k_b \approx 300 \text{ sec}^{-1}$  in the absence of  $\text{Mg}^{2+}$  and nucleotides.

## Values of Kinetic Parameters

Some of the rate constants and equilibrium constants of the reaction scheme of Fig. 15 can be taken from the literature, as summarized in the Table. These assignments of numerical values have to be considered as tentative, however, since the kinetic parameters have been determined with Na,K-ATPase from different sources, such as brain or kidney medulla. In a few cases, literature values of kinetic parameters have been modified in order to improve the fit to the experimental results (Table). The values of  $q_f$  and  $s_f$ , for which no experimental estimates are available, have been adjusted.

Assuming that the ion-binding sites are identical and independent (Robinson, 1983), equilibrium dissociation constants of  $\text{Na}^+$  and  $\text{K}^+$  at the cytoplasmic side are given by

$$K'_{N1} = \frac{1}{3} K'_N; K'_{N2} = K'_N; K'_{N3} = 3K'_N \quad (23)$$

$$K'_{K1} = \frac{1}{2} K'_K; K'_{K2} = 2K'_K. \quad (24)$$

Analogous relations hold at the extracellular side. The factors 1/3, 3, 1/2 and 2 are the usual statistical factors describing binding equilibria in a system with multiple binding sites (Tanford, 1961). For a more detailed discussion of  $\text{Na}^+$ - and  $\text{K}^+$ -binding the Na,K-ATPase, see Karlish and Stein (1985) and Karlish, Rephaeli and Stein (1985). Numerical values of  $K'_N, K''_N, K'_K, K''_K$  have been estimated from the  $\text{Na}^+$ - and  $\text{K}^+$ -concentration dependence of the ATP-hydrolysis rate of Na,K-ATPase (Skou, 1975), as described previously (Läger & Apell, 1986).

## Numerical Simulations

Numerical simulations of the reaction model of Fig. 15 were carried out under the conditions of the dif-

<sup>i</sup> From  $a_b \approx 20 \text{ sec}^{-1}$  and an effective value of the equilibrium dissociation constant of  $a_b/a_f \approx 2 \mu\text{M}$ , accounting for competition with caged ATP. The experimental value of  $a_b/a_f$  is of the order of  $0.1 \mu\text{M}$  (Robinson & Flashner, 1979).

<sup>k</sup> Estimated by fitting Eq. (9) to the observed time course of  $I_p$ . Glynn and Karlish (1976) reported a value of  $r_f \approx 5 \text{ sec}^{-1}$  at  $20^\circ\text{C}$ .

<sup>l</sup> Calculated from Eq. (11), using the values of  $p_f, p_b, \dots$  given in the Table.

<sup>m</sup> From optical determinations of rates of conformational transitions at  $20^\circ\text{C}$ , Karlish (1980) estimated  $h_f$  and  $h_b$  to be about 0.3 and  $300 \text{ sec}^{-1}$ , respectively. Glynn and Richards (1982) observed a rate constant  $h_f$  of spontaneous deocclusion of  $\text{Rb}^+$  of about  $0.2 \text{ sec}^{-1}$  at  $20^\circ\text{C}$ ; a similar value ( $0.1 \text{ sec}^{-1}$ ) was recently reported by Forbush (1987b).

ferent experiments described above. Since the concentrations of ADP and inorganic phosphate built up by hydrolysis of ATP are negligible within the time of the experiment,  $c_D$  and  $c_P$  were set equal to zero throughout. The same set of parameter values, as given in the Table, was found to reproduce, at least qualitatively, the shape of the observed fluorescence and current signals. We have not attempted an optimal fit to the experimental data, but rather have tried to carry out the analysis with a minimal number of assumptions. In particular, we have assumed that the different states of the cycle can be grouped into three classes with respect to the intrinsic fluorescence  $\varphi_i$  [Eq. (5)]:

$\varphi_1$ : {all  $E_1$  states, including  $(\text{Na}_3)E_1 - P$ }

$\varphi_2$ : {all  $P - E_2$  states}

$\varphi_3$ :  $\{E_2(\text{K}_2)$  and  $\text{ATP} \cdot E_2(\text{K}_2)\}$ .

The introduction of only three different fluorescence parameters  $\varphi_1$ ,  $\varphi_2$  and  $\varphi_3$  corresponds to the notion that the fluorescence of the chromophore is mainly determined by the conformational state of the protein and is insensitive to the binding of ligands ( $\text{Na}^+$ ,  $\text{K}^+$ , ATP). The assumption that the conformational state with occluded sodium has the same fluorescence as state  $E_1$  is based on the finding that chymotrypsin modification of the protein, which blocks deocclusion of  $\text{Na}^+$ , abolishes the fluorescence change.

According to Eq. (6), the time course of  $\Delta F/F_0$  is determined by the relative fluorescence increments  $f_i \equiv (\varphi_i - \varphi_1)/\varphi_1$ . Since  $f_i$  is referred to fluorescence state 1 (containing all  $E_1$  states), the relation

$$f_1 \equiv 0 \quad (25)$$

holds. According to the assumption introduced above,  $f_2$  and  $f_3$  are given by:

$$f_2 = f(P - E_2 \cdot \text{Na}_i) = f(P - E_2 \cdot \text{K}_j) \quad (26)$$

$$(i = 0, 1, 2, 3; j = 1, 2)$$

$$f_3 = f(E_2(\text{K}_2)) = f(\text{ATP} \cdot E_2(\text{K}_2)). \quad (27)$$

Introducing into Eq. (6) the variables  $x_i$  defined in Appendix A,  $\Delta F/F_0$  can be represented by

$$\frac{\Delta F}{F_0} = \frac{f_2(x_4 - x_{40}) + f_3(x_{55} - x_{50} + x_6 - x_{60})}{1 + f_2x_{40} + f_3(x_{50} + x_{60})}. \quad (28)$$

For fitting Eq. (28) to the experimental data, the following values of  $f_2$  and  $f_3$  have been used:

$$f_2 = -0.027; f_3 = -0.14. \quad (29)$$

$f_2$  has been evaluated from the experiments in the absence of  $\text{K}^+$ . Using the value of  $f_2$ ,  $f_3$  is obtained from the fluorescence signal in the presence of  $\text{Na}^+$  and  $\text{K}^+$ .

With these values of  $f_2$  and  $f_3$  and with the parameters of the Table, the simulated fluorescence signals are found to reproduce approximately the time course of the signals recorded under the various experimental conditions. The results of the simulations are compared in Figs. 6, 8 and 10 with the experimental data. As seen from Fig. 6, the calculated dependence of signal amplitude  $a_F$  and half-time  $t_{1/2}$  on  $\text{Na}^+$  concentration  $c_N$  under  $\text{K}^+$ -free conditions agrees well with the experimental findings. At low  $c_N$  the rate of the  $E_1 \rightarrow E_2$  transition is limited by the low concentration of  $\text{Na}_3 \cdot E_1$ , and  $t_{1/2}$  is large. On the other hand, at saturating  $\text{Na}^+$  concentrations, the time  $t_{1/2}$  is determined by the rate of the deocclusion step  $(\text{Na}_3)E_1 - P \rightarrow P - E_2 \cdot \text{Na}_3$  (rate constant  $l_p$ ); accordingly,  $t_{1/2}$  approaches a constant value  $(\ln 2)/l_p \approx 40$  msec at large  $c_N$ .

The low rate of the  $E_1 \rightarrow E_2$  transition at small  $c_N$  also explains the sodium-concentration dependence of  $a_F$  (Fig. 6A), in the following way. For  $c_N \rightarrow 0$ , the rate of transitions  $\text{Na}_3 \cdot E_1 \cdot \text{ATP} \rightarrow (\text{Na}_3)E_1 - P \rightarrow P - E_2$  becomes comparable to the rate of spontaneous dephosphorylation ( $P - E_2 \rightarrow E_1$ , rate constant  $r_f \approx 1 \text{ sec}^{-1}$ ). Under this condition, when the formation rate of  $P - E_2$  is of the same order or smaller than the rate of decay back to conformation  $E_1$ , ATP release to the solution can only slightly shift the  $E_1/E_2$  concentration ratio. This means that the signal amplitude  $a_F$  must vanish for  $c_N \rightarrow 0$ . On the other hand, at high  $c_N$ , where a large fraction of pump molecules accumulates in state  $E_2$  after phosphorylation,  $a_F$  approaches the limiting value  $f_2 = -0.027$  (Fig. 6A).

In the presence of both  $\text{Na}^+$  and  $\text{K}^+$ , the amplitude  $-a_F$  of the fluorescence signal is increased compared to the experiments with  $\text{K}^+$ -free media (Fig. 8). On the basis of the reaction scheme of Fig. 15, the increase of  $-a_F$  is explained assuming that in the presence of  $\text{K}^+$ , the pump enters state  $E_2(\text{K}_2)$  which has a lower fluorescence than  $P - E_2$ . The observed saturation of  $a_F$  with increasing  $\text{K}^+$ -concentration, which reflects high-affinity binding of  $\text{K}^+$  to state  $P - E_2$ , agrees with the predictions from numerical simulations (Fig. 8B). The  $\text{K}^+$ -concentration dependence of the half-time  $t_{1/2}$  is also reproduced by the simulated fluorescence signals (Fig. 8A).

An alternative explanation for the difference in signal amplitude with and without  $\text{K}^+$  could consist in the assumption that  $f_2$  and  $f_3$  are nearly equal, but that in the absence of  $\text{K}^+$  an appreciable fraction of the enzyme remains in state  $(\text{Na}_3)E_1 - P$  after phosphorylation (Steinberg & Karlisch, 1989). This possi-



bility seems unlikely, however, since in the absence of  $K^+$  the signal amplitude was the same with 20 and 150 mM  $Na^+$ . Furthermore, assuming  $f_2 \approx f_3$ , we were unable to fit the observed dependence of  $t_{1/2}$  on potassium concentration  $c_K$  (Fig. 8B).

In experiments with sodium-free potassium media, the half-time  $t_{1/2}$  of the fluorescence signal is found to decrease with increasing  $K^+$  concentration  $c_K$ , whereas the signal amplitude  $a_F$  reaches a maximum and decreases again at large  $c_K$  (Fig. 10). This behavior is also seen in the simulated fluorescence signals, as Fig. 10 shows. The origin of the maximum in  $a_F = f(c_K)$  may be explained in the following way. After the concentration jump, ATP binds to state  $E_2(K_2)$ , inducing transitions  $ATP \cdot E_2(K_2) \rightarrow K_2 \cdot E_1 \cdot ATP$ . At intermediate  $K^+$  concentrations, the newly formed state  $K_2 \cdot E_1 \cdot ATP$  is rapidly depopulated by dissociation of  $K^+$ , and virtually all initially present  $E_2(K_2)$  is transformed into  $E_1$ , leading to a large fluorescence increase. At high  $K^+$ -concentration, however, a large proportion of the enzyme remains in state  $K_2 \cdot E_1$  after the  $E_2 \rightarrow E_1$  transition, from which it can return, with a rate constant  $h_b \approx 250 \text{ sec}^{-1}$ , back to  $E_2(K_2)$ . This reduces the net amount of enzyme which undergoes the transition from  $E_2(K_2)$  to  $E_1$ , and thus the amplitude  $a_F$ .

From the time-dependent pump current  $I_p(t)$  the translocated charge  $Q(t)$  can be evaluated. In Fig. 12 the experimental values of  $Q$  are compared with the charge  $Q_{sim}$  predicted by numerical simulation of the reaction cycle. The time course of  $Q_{sim}$  critically depends on the assumptions regarding the nature of the electrogenic steps. A satisfactory agreement between  $Q(t)$  and  $Q_{sim}(t)$  is found, assuming that formation of the occluded state ( $Na_3 \cdot E_1 \cdot ATP \rightarrow (Na_3)E_1-P$ ) is an electrically silent process. This means that the main charge-translocating events are the deocclusion step and/or the release of  $Na^+$  to the extracellular medium. The calculation of  $Q_{sim}$  was carried out with the parameter values of the Table, together with the following assignments of the dielectric coefficients. According to the finding that the reactions prior to the formation of the occluded state are electrically silent,  $\alpha'$  and  $\alpha_i$  (Eq. 17) were set equal to zero. Assuming that the major electrogenic event is the deocclusion step,  $\alpha_p$  was set equal to unity and  $\alpha''$  equal to zero. (Since release of  $Na^+$  is assumed to be fast,  $Q_{sim}$  is insensitive to the choice of  $\alpha_p$  and  $\alpha''$ , as long as the sum  $\alpha_p + \alpha''$  remains constant.) From Eqs. (16), (17) and (20), it is seen that these assignments are equivalent to setting  $\beta' = 1$ ,  $\beta'' = 0$  and  $z_L = -2$ . The coefficients  $\alpha_k$  and  $\alpha_q$  (Eqs. (18) and (19)) are not to be specified, since the rate of the corresponding reactions vanishes in the absence of  $K^+$ . Furthermore, since the translocated charge is obtained

from the difference  $I_p - I_p^\infty$  (Eq. (3)), the coefficient  $\alpha_f$  describing the back reaction responsible for the quasistationary pump-current  $I_p^\infty$  was set equal to zero. As seen from Fig. 12, the simulated and the observed time-course of translocated charge closely agree.

## Discussion

Concentration-jump relaxation experiments yield information on the kinetic properties of an ion pump which cannot easily be obtained by other methods. In this study we have attempted to correlate transient electrical events in the Na,K-pump with conformational transitions elicited by an ATP-concentration jump. When the medium contains  $Na^+$ , but no  $K^+$ , the fluorescence of the 5-IAF-labeled protein decreases monotonously after activation by ATP. In parallel experiments carried out under otherwise identical conditions with membrane fragments bound to a planar bilayer, a transient pump current  $I_p(t)$  was observed which decayed with nearly the same time behavior. Apart from a scaling factor, the fluorescence signal  $\Delta F(t)/F_0$  was found to nearly superimpose with the time integral  $Q(t)$  of  $I_p$  (Fig. 12). The close correlation between  $\Delta F/F_0$  and  $Q(t)$  indicates that the optical and the electrical transient are governed by the same rate-limiting step. Chymotrypsin modification of the protein, which is known to block the transition from  $(Na_3)E_1-P$  to  $P-E_2 \cdot Na_3$ , was found to eliminate both the fluorescence signal and the current transient. This strongly suggests that the fluorescence change as well as the charge movement take place after formation of the occluded state, i.e., in the transitions  $(Na_3)E_1-P \rightarrow P-E_2 \cdot Na_3 \rightarrow P-E_2$ . Assuming that release of sodium ( $P-E_2 \cdot Na_3 \rightarrow P-E_2$ ) is fast, the experimentally observed time constant of the fluorescence decay may be identified with the chemical relaxation time of the transition  $(Na_3)E_1-P \rightleftharpoons P-E_2 \cdot Na_3$ .

In experiments with  $Na^+$ -free  $K^+$ -media, an inverse fluorescence change is observed after the ATP-concentration jump, which is likely to be associated with the transition  $E_2(K_2) \rightarrow K_2 \cdot E_1$ . In contrast to the large electrical signals observed in the presence of  $Na^+$ , no transient current could be detected when the medium contained only  $K^+$ . This finding indicates that the deocclusion step ( $E_2(K_2) \rightarrow K_2 \cdot E_1$ ) is electrically silent. The observation that  $Na^+$  translocation is electrogenic, whereas  $K^+$  translocation is electrically silent, can be explained assuming that the alkali-ion binding site of the protein bears a charge of  $-2e_0$ , corresponding to a net charge of  $+e_0$  in the sodium-loaded form and a net charge of zero in the potassium-loaded form

(Goldshlegger et al., 1987; DeWeer, Gadsby & Roakowsky, 1988; Läuger & Apell, 1988).

After the transition  $E_2(K_2) \rightarrow K_2 \cdot E_1$ ,  $K^+$  ions are released to the cytoplasmic medium. Under the conditions of the experiment of Fig. 13 ( $c_K = 2$  mM), net release occurs since the  $K^+$  affinity in state  $E_1$  is low ( $K'_K \approx 20$  mM). The release step,  $K_2 \cdot E_1 \rightarrow E_1$ , could be associated with charge translocation, if the  $K^+$  ions move in a narrow, low-conductance access channel ("ion well") connecting the binding site with the aqueous medium. The fact that no charge translocation is observed in the experiments with  $Na^+$ -free  $K^+$  media provides strong arguments against the existence of a potassium well at the cytoplasmic side. It cannot be excluded, however, that a low-conductance access channel is present at the extracellular face of the pump.

It is well known (Glynn, 1985) that in the simultaneous presence of  $Na^+$  and  $K^+$ , the phosphorylated state  $P-E_2$  undergoes a rapid transformation into the occluded state  $E_2(K_2)$  via the reaction sequence  $P-E_2 \cdot Na_3 \rightarrow P-E_2 \cdot K_2 \rightarrow E_2(K_2)$ . The fluorescence signal, which is observed in the presence of both  $Na^+$  and  $K^+$ , exhibits the same time course as in the absence of  $K^+$ , but the amplitude of the decrease is much larger. These findings may be explained, assuming that  $E_2(K_2)$  has a weaker fluorescence than  $P-E_2 \cdot Na_3$  (Kapakos & Steinberg, 1986a) and that the transitions  $P-E_2 \cdot Na_3 \rightarrow P-E_2 \cdot K_2 \rightarrow E_2(K_2)$  are fast compared with the preceding reaction step ( $Na_3E_1-P \rightarrow P-E_2 \cdot Na_3$ ).

The conclusions that we have drawn from our experiments may be compared with the results of previous studies. From voltage-jump current-relaxation experiments with cardiac cells, Nakao and Gadsby (1986) proposed that translocation of  $Na^+$  is a major charge-carrying step in the pumping cycle of the Na,K-ATPase. Similar experiments gave evidence that translocation of  $K^+$  is an electrically silent process (Bahinski, Nakao & Gadsby, 1988). Essentially the same conclusion has been drawn by Goldshlegger et al. (1987) from the finding that in reconstituted vesicles potassium-potassium exchange is voltage insensitive. These observations basically agree with the results of the present study.

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## Appendix A

### Numerical Simulation of the Reaction Cycle of Fig. 15

We denote the fraction of pump molecules in state *A* by *x*[*A*] and introduce the following variables:

$$x_1 \equiv x[\text{Na}_3 \cdot E_1] + x[\text{Na}_2 \cdot E_1] + x[\text{Na} \cdot E_1] + x[E_1] + x[\text{K} \cdot E_1] + x[\text{K}_2 \cdot E_1] \quad (\text{A1})$$

$$x_2 \equiv x[\text{Na}_3 \cdot E_1 \cdot \text{ATP}] + x[\text{Na}_2 \cdot E_1 \cdot \text{ATP}] + x[\text{Na} \cdot E_1 \cdot \text{ATP}] + x[E_1 \cdot \text{ATP}] + x[\text{K} \cdot E_1 \cdot \text{ATP}] + x[\text{K}_2 \cdot E_1 \cdot \text{ATP}] \quad (\text{A2})$$

$$x_3 \equiv \chi[(\text{Na}_3)E_1 - P] \quad (\text{A3})$$

$$x_4 \equiv x[P - E_2 \cdot \text{Na}_3] + x[P - E_2 \cdot \text{Na}_2] + x[P - E_2 \cdot \text{Na}] + x[P - E_2] + x[P - E_2 \cdot \text{K}] + x[P - E_2 \cdot \text{K}_2] \quad (\text{A4})$$

$$x_5 \equiv x[E_2(\text{K}_2)] \quad (\text{A5})$$

$$x_6 \equiv x[\text{ATP} \cdot E_2 \cdot (\text{K}_2)] \quad (\text{A6})$$

$$x_1 + x_2 + x_3 + x_4 + x_5 + x_6 = 1. \quad (\text{A7})$$

According to Fig. 15, the rate of change of *x*<sub>1</sub> is given by

$$\dot{x}_1 = -(a_f c_T + h_b k'_1 k'_2 / P' + r_b c_P / P') x_1 + a_b x_2 + (r_f / P'') x_4 + h_f x_5. \quad (\text{A8})$$

Analogous equations hold for  $\dot{x}_2, \dot{x}_3, \dots, \dot{x}_6$ .

In Eq. (A8) the following relations have been used which are obtained from Eqs. (10) and (11):

$$x[E_1] = \frac{x_1}{P'}; \quad x[\text{K}_2 \cdot E_1] = \frac{k'_1 k'_2}{P'} x_1$$

$$x[P - E_2] = \frac{x_4}{P''} \quad (\text{A9})$$

$$P' \equiv 1 + n'_1 + n'_1 n'_2 + n'_1 n'_2 n'_3 + k'_1 + k'_1 k'_2 \quad (\text{A10})$$

$$P'' \equiv 1 + n''_1 + n''_1 n''_2 + n''_1 n''_2 n''_3 + k''_1 + k''_1 k''_2. \quad (\text{A11})$$

The differential equations for  $\dot{x}_1, \dots, \dot{x}_6$  may be numerically integrated using a Runge-Kutta algorithm. In this way the time course of the fluorescence signal  $\Delta F/F_0$  may be evaluated using Eq. (3).